



**BANCO CENTRAL DO BRASIL**

Working Paper Series

106

**Testing Nonlinearities Between Brazilian  
Exchange Rate and Inflation Volatilities**

*Christiane R. Albuquerque and Marcelo S. Portugal*  
May, 2006

Working Paper Series	Brasília	n. 106	May	2006	P. 1-41
----------------------	----------	--------	-----	------	---------

# *Working Paper Series*

Edited by Research Department (Depep) – E-mail: [workingpaper@bcb.gov.br](mailto:workingpaper@bcb.gov.br)

Editor: Benjamin Miranda Tabak – E-mail: [benjamin.tabak@bcb.gov.br](mailto:benjamin.tabak@bcb.gov.br)

Editorial Assistant: Jane Sofia Moita – E-mail: [jane.sofia@bcb.gov.br](mailto:jane.sofia@bcb.gov.br)

Head of Research Department: Carlos Hamilton Vasconcelos Araújo – E-mail: [carlos.araujo@bcb.gov.br](mailto:carlos.araujo@bcb.gov.br)

The Banco Central do Brasil Working Papers are all evaluated in double blind referee process.

Reproduction is permitted only if source is stated as follows: Working Paper n. 106.

Authorized by Afonso Sant'Anna Bevilaqua, Deputy Governor of Economic Policy.

## **General Control of Publications**

Banco Central do Brasil

Secre/Surel/Dimep

SBS – Quadra 3 – Bloco B – Edifício-Sede – M1

Caixa Postal 8.670

70074-900 Brasília – DF – Brazil

Phones: (5561) 3414-3710 and 3414-3567

Fax: (5561) 3414-3626

E-mail: [editor@bcb.gov.br](mailto:editor@bcb.gov.br)

The views expressed in this work are those of the authors and do not necessarily reflect those of the Banco Central or its members.

Although these Working Papers often represent preliminary work, citation of source is required when used or reproduced.

*As opiniões expressas neste trabalho são exclusivamente do(s) autor(es) e não refletem, necessariamente, a visão do Banco Central do Brasil.*

*Ainda que este artigo represente trabalho preliminar, citação da fonte é requerida mesmo quando reproduzido parcialmente.*

## **Consumer Complaints and Public Enquiries Center**

Address: Secre/Surel/Diate

Edifício-Sede – 2º subsolo

SBS – Quadra 3 – Zona Central

70074-900 Brasília – DF – Brazil

Fax: (5561) 3414-2553

Internet: <http://www.bcb.gov.br/?english>

# Testing Nonlinearities Between Brazilian Exchange Rate and Inflation Volatilities<sup>\*</sup>

Christiane R. Albuquerque<sup>\*\*</sup>

Marcelo S. Portugal<sup>\*\*\*</sup>

## Abstract

*The Working Papers should not be reported as representing the views of the Banco Central do Brasil. The views expressed in the papers are those of the author(s) and do not necessarily reflect those of the Banco Central.*

There are few studies directly addressing exchange rate and inflation volatilities, and lack of consensus among them. However, this kind of study is necessary, especially because they can help monetary authorities to know price behavior better. This article analyses the relation between exchange rate and inflation volatilities using a bivariate GARCH model, and therefore modeling conditional volatilities, fact largely unexplored by the literature. We find a semi-concave relation between those series, and this nonlinearity may explain their apparently disconnection under a floating exchange rate system. The article also shows that traditional tests, with non-conditional volatilities, are not robust.

**Keywords:** Exchange rate, inflation, volatility, Garch models

**JEL classification:** E31, F41

---

<sup>\*</sup> The authors would like to thank Carlos H. V. Araújo, Joaquim de Andrade, Maria da Glória Araújo, Roberto Campos de Moraes, Sergio Lago and an anonymous referee for their comments on a previous version. The authors also would like to thank Angelo Fasolo and Eui Jung for their valuable contributions to this paper. The remaining errors are the authors' responsibility.

<sup>\*\*</sup> Research Department, Banco Central do Brasil. E-mail: [christiane.albuquerque@bcb.gov.br](mailto:christiane.albuquerque@bcb.gov.br)

<sup>\*\*\*</sup> Professor of Economics, Universidade Federal do Rio Grande do Sul (UFRGS), and associate researcher of CNPq. Email: [msp@ufrgs.br](mailto:msp@ufrgs.br)

## 1. Introduction

The study of exchange rate volatility's effects should be important for monetary policy decisions, since higher volatility means higher uncertainty, which may affect inflation expectations, a crucial variable in monetary policy decisions. Although the literature about the impact of exchange rate volatility on inflation is not as extensive as the one available for its pass-through to prices, some authors highlight such relation. Whether the impacts are significant or not remains controversial: some authors defend the absence of connection between exchange rate and macroeconomic variables volatilities, while others state the opposite<sup>1</sup>. According to the first group, exchange rate volatility is not important to macroeconomic variables, since empirical evidence shows a substantial increase in the former during floating exchange rate regimes, while the latter did not present a similar rise in their volatilities<sup>2</sup>. The second group finds evidence of such relation, being either positive or negative, in studies conducted under different aims and approaches.

This paper tests the existence of a relation between exchange rate and inflation volatilities for the Brazilian case, and our conclusions in this paper could be classified in the second group, related especially with the findings of Dixit (1989) and Seabra (1996). By developing an optimization model for the firm, the first author shows that trade flows and prices would depend on investment made on a future basis and, consequently, on both expectations and higher moments of the distributions involved. In consequence, the macroeconomic environment affects the pattern of price changes. Hence, not only the level of the devaluation but also the volatility of the exchange rate would affect its pass-through to prices. Seabra (1996), on its turn, uses a model of intertemporal optimization with asymmetric adjustment costs and shows that the critical value that leads a firm to invest is a function of uncertainty. If uncertainty is high, the optimal decision will be to wait before making a movement (wait-and-see strategy), even with the exchange rate at a level that makes investment profitable. This attitude impacts on aggregate supply and, therefore, on inflation.

---

<sup>1</sup> For the first group, see, for instance, Krugman (1998), Obstfeld and Rogoff (2000), Baxter and Stockman (1988), Flood and Rose (1995), Obstfeld and Rogoff (2000), Rogoff (2001) and Duarte and Stockman (2002). For the second, Calvo and Reinhart (2000a, 2000b), Barkoulas, Baum and Cavaglan (2002), Wei and Parsley (1995), Andersen (1997), Smith (1999), Engel and Rogers (2001), Devereux and Engel (2003) and Chen (2004), Chen (2004), Barone-Adesi and Yeung (1990), Bleaney (1996), and Bleaney and Fielding (2002).

<sup>2</sup> Obstfeld and Rogoff (2000) call the apparently disconnection between the exchange rate volatility and macroeconomic fundamentals as the exchange rate disconnect puzzle (ERDP).

Other interesting works are those of Haussmann, Panizza and Stein (2001), who find a negative and significant correlation in their tests between pass-through and measures of volatility, and Smith (1999), where a reduction in inflation volatility as a result of an increase in exchange rate volatility was found in approximately 31% of the cases. The welfare approach recalled by Ghosh, Gulde, Ostry and Holger (1997) and by Sutherland (2002) are also worth mentioning. The former show that inflation volatility is lower under floating and intermediate exchange rate regimes for countries with low inflation, while the latter show that the sign of the relation between exchange rate and inflation volatilities will depend on the model's parameters.

In this paper, we adopt a more sophisticated econometric methodology than those applied so far in literature: instead of constructing exogenous volatility series (by computing the volatility of subsamples or rolling windows) we apply a bivariate GARCH model, working with conditional volatility series. The purpose of this procedure is to adopt a measure not sensitive to individual selection criteria. Apart from that, by modeling the conditional heteroskedasticity of exchange rates, it is also a more suitable econometric technique. One of the contributions proposed by this paper is to verify whether exchange rate volatility has impacts strong enough on inflation so that the monetary authority should monitor it, an approach still scarce, especially in Brazil. The other one is to show that traditional tests are not robust for this type of study and that Garch-type models are more suitable for such analysis.

The paper is divided into six sections, including this introduction. Section 2 introduces the theoretical model that led to the econometric tests, while data is presented in section 3. The results obtained by the use of traditional methods (i.e.: unconditional variance series) are presented in section 4. Section 5 shows the results of the bivariate GARCH model, and section 6 concludes.

## 2. The theoretical model

We derive an equation relating inflation and exchange rate volatilities to test for the existence of a significant relation between them. The approach to achieve such equation is based on Bleaney and Fielding (2002), with slight modifications. The government has a utility function  $Z$ , of the Barro and Gordon (1983) type, to be maximized.  $Z$  is given by equation (1), which represents the case where the government of a country faces a trade-off between price stabilization and output growth above its equilibrium level.

$$Z = -0.5\pi^2 - 0.5b(y - y^* - k)^2 \quad (1)$$

Where  $\pi$  is inflation,  $y$  is the output level and  $y^*$  is potential output. The term  $b > 0$  is incorporated by the authors, meaning the relative weight given to output, and  $k > 0$  represents the inflationary bias of the government. The presence of  $b$  and  $k$  comes from the assumption that a government could eventually attribute a higher weight to output growth to the detriment of price stability.

The restriction imposed by the authors upon function  $Z$  consists of an expectations-augmented Phillips Curve, including the exchange rate. Here, we have the first difference to the model of Bleaney and Fielding (2002) since we will focus not on the real but on the nominal exchange rate. Our restriction will be a Phillips Curve for an open economy, including both the forward-looking and the backward-looking term, as described in equation (2) below.

$$\pi_t = a_o \pi_t^e + a_1 \pi_{t-1} + a_2 (y - y^*) + a_3 \Delta(p_t^{ext}) + a_4 s_t + \varepsilon_t \quad (2)$$

where  $p_t^{ext}$  is the foreign price level,  $s_t$ , the nominal exchange rate and  $\pi_t^e$  the inflation expectation between period  $t$  and period  $t+1$ .

We also assume the exchange rate following a random walk, as in many partial equilibrium studies. Thus, we have

$$s_t = s_{t-1} + \eta_t \quad \eta_t \sim N(0, \sigma^2_{\eta}) \quad (3)$$

applying (2) and (3) to (1), and obtaining the first-order condition for the maximization of  $Z$  with respect to  $\pi$ , we have

$$\pi = \beta a_o \pi_t^e + \beta a_1 \pi_{t-1} + \beta a_3 \Delta p_t^{ext} + \beta a_4 s_{t-1} + \beta a_4 \eta_t + \beta \varepsilon_t + K' \quad (4)$$

where  $\beta = \frac{b}{a_2^2 + b}$  and  $K' = -\beta a_2 k$

Some assumption also must be made concerning the behavior of  $\pi_t^e$ . We, then, consider that inflation expectations are of the form:

$$\pi_t^e = \pi_{t-1} + v_t \quad (5)$$

Thus, substituting (5) in (4) we get that

$$E[\pi] = (\beta a_o + \beta a_1) \pi_{t-1} + \beta a_3 \Delta p_t^{ext} + K' \quad (6)$$

The terms  $\varepsilon_t$ ,  $\eta_t$  and  $v_t$  are independents, therefore, inflation variance given by

$$\text{var}(\pi) = \beta^2 a_o^2 E(v_t)^2 + \beta^2 a_4^2 E(\eta_t)^2 + \beta^2 E(\varepsilon_t)^2 \quad (7)$$

But, from (2), we have that  $E(\varepsilon_t)^2$  is the inflation variance. Hence,

$$\text{var}(\pi) = \mu_0 E(v_t)^2 + \mu_1 E(\eta_t)^2 \quad (8)$$

where  $\mu_0 = \frac{\beta^2 a_o^2}{(1-\beta^2)}$  and  $\mu_1 = \mu_0 * \frac{a_4^2}{a_o^2}$

Inflation variance is, therefore, a function of  $v_t$  (the variance of the shock expected in  $t$  in relation to  $t-1$  inflation) and of  $\eta_t$  (variance of the exchange rate process).

With (8), we may test for a relation between volatilities and we aim to do that by using a multivariate GARCH model. However, due to the small sample available – from the beginning of the floating exchange rate system in Brazil, i.e., January, 1999 to September, 2004 – the large number of terms to be estimated does not allow us to estimate a multivariate GARCH model with three variables. Aside from that, the inflation expectations research published by the Central Bank of Brazil started only on April, 2000, reducing our sample even further. Therefore, we will assume that the variance measured by  $v_t$  is constant and, hence, equation (8) becomes:

$$\text{Var}(\pi) = \mu'_0 + \mu_1 \text{var}(\eta_t),$$

where  $\mu'_0 = \mu_0 + \text{var}(v_t)$  is the new constant.

Although the assumption that  $v_t$  is constant is strong, we may consider it. Table 1 shows the result of a regression of  $\pi_t^e$  against  $\pi_{t-1}$  and a constant. If our hypothesis that the shock expected to  $t+1$  in comparison with  $t-1$  is, on average, constant, then the residuals of this equation should be homoskedastic. As we may see, we accept the null hypothesis of homoskedasticity, which supports our assumption that  $v_t$  is constant.<sup>3</sup> Besides, if we compute  $v_t = \pi_t^e - \pi_{t-1}$  one can notice that almost the entire series is within the interval of one standard deviation from the mean, as shown in Graph 1, with the longest period in which it was outside that band being from December 2002 to April 2003.

The data for  $\pi_t^e$  refer to the average market expectations for IPCA<sup>4</sup> inflation in month  $t+1$  as in the last business day of month  $t-1$ , and they are published by the Investor Relations Group (Gerin) from the Central Bank of Brazil.<sup>5</sup>

Table 1: Estimation of Equation  $\pi_t^e = c + \pi_{t-1}$

<i>method: OLS; sample: 2000:03 to 2004:10</i>				
Variable	Coefficient	Standard deviation	t-statistics	p-value
$\pi_{t-1}$	0.1593	0.0542	2.9385	0.0049
C	0.4463	0.0555	8.0351	0.0000
MA(1)	0.6576	0.1145	5.7452	0.0000
$R^2$	0.4584	Durbin-Watson		1.8755
adjusted $R^2$	.4376	White Test for homoskedasticity: (p-value)		0.4354

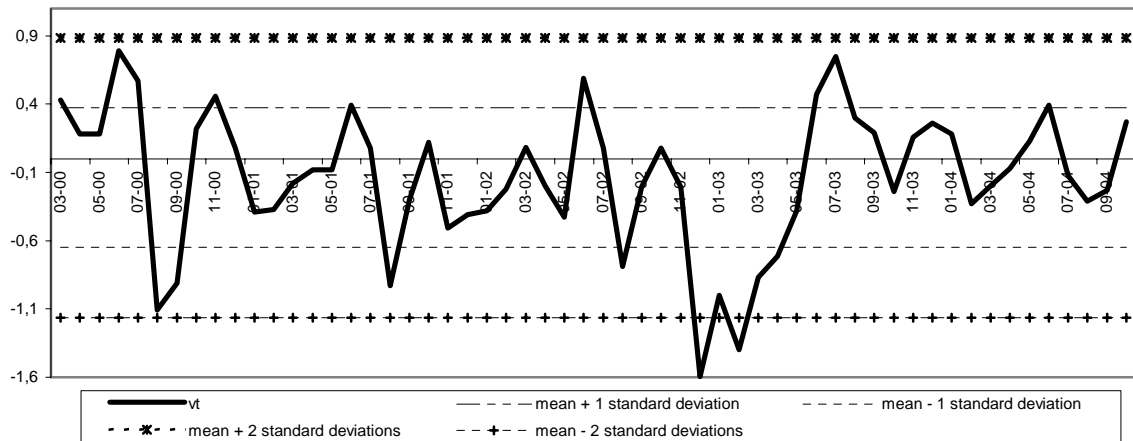
<sup>3</sup> Equivalent tests to  $\pi_t$  and  $s_t$  from equations 2 and 3 accepted the alternative hypothesis of heteroskedasticity.

<sup>4</sup> Index of consumer prices considered by the Central Bank in the inflation targeting.

<sup>5</sup> <http://www4.bcb.gov.br/?FOCUSERIES>



Graph 1 – Evolution of  $v_t = \pi^e - \pi_{t-1}$



### 3. Data

Our sample was computed on a monthly basis, from 1999:01 to 2004:09, and data used in our estimations were the following:

- Price Index: Extended Consumer Price Index (IPCA), consumer price index published by the Brazilian Institute of Geography and Statistics (IBGE),<sup>6</sup> December/1993=100 and considered by the Central Bank of Brazil as the reference index in the inflation targeting regime;
- Exchange Rate: Exchange rate R\$/US\$, selling prices, monthly average;
- External Prices: *Producer price index* (PPI), published by the *Bureau of Labour Statistics*<sup>7</sup> (commodities, final goods).
- GAP: output gap. It was computed by subtracting the industrial production series published by IBGE (used as a *proxy* for monthly GDP) from the trend obtained by the Hodrick-Prescott filter.

All series were seasonally adjusted by the X-12 method and, afterwards, taken in logarithms (ln). Next, unit root tests were performed. All series, except for *gap* have unit roots, as shown in Table A1 in the appendix I, and, therefore, they were taken in first differences. The series in first difference of *Price Index*, *Exchange Rate* and *External Prices* are henceforth referred to as *IPCA*, *E* and *PPI*, respectively.

<sup>6</sup> <http://www.ibge.gov.br>

<sup>7</sup> <http://www.bls.gov/data>

#### 4. Tests with unconditional volatility

As a first step, we followed the main procedures found in literature and made tests using unconditional volatilities. In such cases, volatility is more often computed by the standard deviation from the mean in small samples, or by the variance within them. These samples are given either by splitting the series into small subsamples or by adopting rolling windows<sup>8</sup>.

In this paper, we opted for three different methods to calculate the unconditional volatility series. The first one is constructed by computing the standard deviation from the mean in rolling windows with 4, 6, 8 and 12 observations in each window (series are computed as the first difference of the natural logarithm of the variable on a monthly basis). The second one considers the variances, instead of the standard deviation. Finally, we tested a VAR between the price index (IPCA) and the exchange rate (E) and analyzed the resulting variance decomposition.

##### 4.1. Rolling Windows with standard deviations

The volatilities computed by the standard deviations are presented in Graphs 2 and 3, where  $E_i$  and  $IPCA_i$  are the volatilities of E and IPCA, respectively, within a window of size  $i$ . It is possible to note that the series are sensitive to the size of the window. As Table A.2 shows, the unit root test for  $IPCA_i$  is also affected by window size:  $IPCA_4$  is stationary and so is  $IPCA_6$ , although we reject the presence of unit roots in the former at a level of significance of 10%. However,  $IPCA_8$  and  $IPCA_{12}$  have unit roots. Since  $E_i$  is always stationary, we computed the first differences of  $IPCA_8$  and  $IPCA_{12}$ , named  $d\_IPCA_8$  and  $d\_IPCA_{12}$ , respectively.

The estimation results also are very sensitive to window size, as it can be seen in tables A.3 to A.6 in appendix I<sup>9</sup>. In the four-month window, the lagged terms of a variable in its respective equation and the effect of inflation variance on exchange rate variance are considered

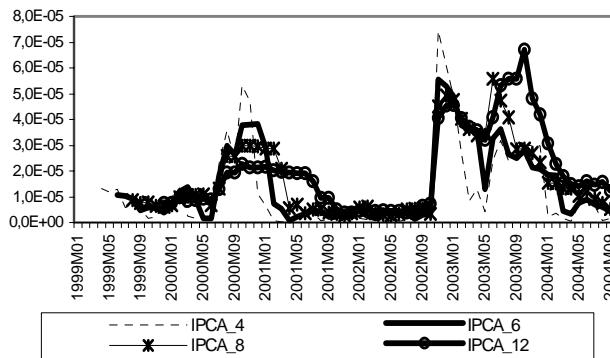
---

<sup>8</sup> Bastourre and Carrera (2004) attribute the few macroeconomic studies about volatility to the lack of a pattern to define or to measure volatility. According to them, the use of *rolling windows*, instead of subsamples, has the advantage of reducing information loss (resultant from the reduced sample size). However, this procedure is also limited due to the difficulty in determining the ideal number of observations in a window. In addition, it may imply a high correlation between the computed series, which may affect the quality of estimators, and alter the true relation between the volatilities. For instance, once the exchange rate regime varies over time, a certain window may contain two different regimes.

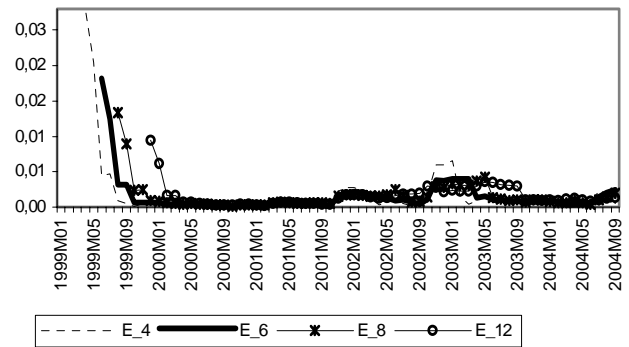
<sup>9</sup> The number of lags in each VAR was chosen by taking into consideration the information criteria, absence of residual autocorrelation (LM test), absence of correlation between variables, and parsimony. In all models the dummy variable  $d2002\_M11$  - which assumes the unity value for November 2002 - was included, since in all series there is a peak in that month, probably associated with the confidence crisis. Its inclusion allowed us to correct problems of residual autocorrelation or correlation between the variables found in the model. For similar reasons, the dummy variables  $d1999$  in the four-month window and  $d2003\_M10$  in the 12-month window were included. The latter assumes the unity value for April and May 1999 (peak in  $E_4$ ) while the former equals the unity value for October 2003 (peak in  $IPCA_{12}$ ).

to be statistically significant. With regard to the six-month window, there are significant cross-terms. However, the Wald test shows that the sum of the lagged coefficients of  $E_6$  in the  $IPCA_6$  equation is not statistically different from zero, and the same happens to the lagged coefficients of  $IPCA_6$  in the  $E_6$  equation. Only the dummy and first lag of a variable are significant in the equation. In the eight-month window, only  $E_8(-1)$  in the equation for  $E_8$  is significant, while only the dummy is significant in the  $D\_IPCA_8$  equation. However, in this VAR, the correlation between  $IPCA_8$  and  $E_8$  equals  $-0.43$ , which may jeopardize the OLS estimation. Finally, the VAR between  $d\_IPCA_{12}$  and  $E_{12}$  reports the coefficient of  $E_{12}(-1)$  as the only significant one in the  $E_{12}$  equation.  $E_{12}(-1)$ ,  $E_{12}(-6)$  and  $E_{12}(-7)$  are significant in the  $d\_IPCA_{12}$  equation and, according to the Wald test, their sum is statistically different from zero at a 10% level.

Graph 2 – Variances of IPCA (standard deviations from the mean) - Rolling Windows



Graph 3 – Variances of E (standard deviations from the mean) - Rolling Windows



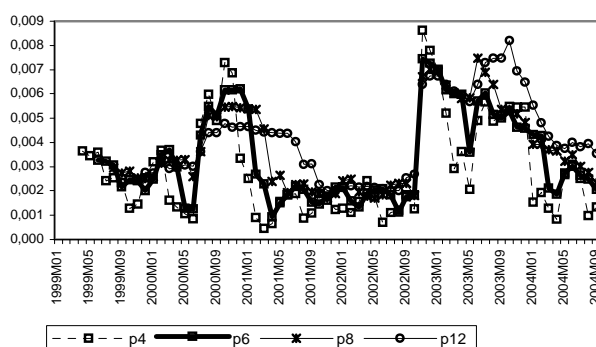
In sum, the relation between those two endogenous variables is sensitive to window size. Depending on the size selected, we may accept or reject that the exchange rate variance affects inflation variance and the other way round, as well as accept or reject that lagged values of inflation variance will affect it.

#### 4.2. Rolling Windows with variances

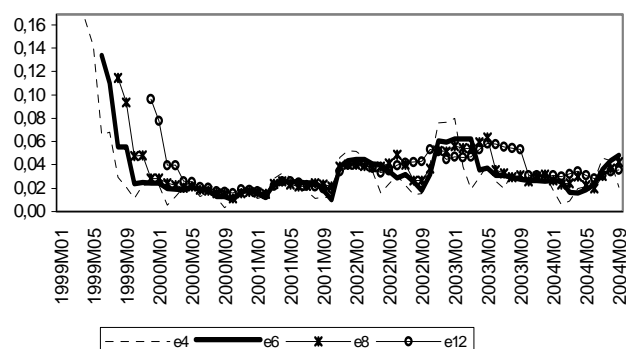
Once again, we have series that are very sensitive to window size, as shown in Graphs 4 and 5 ( $\pi$  and  $e$  are the volatility series for IPCA and E, respectively, computed as the variance of the sample inside the window). Concerning stationarity, the only difference from the standard deviation case is that the variance of IPCA in the six-month window is not stationary (table A.7 in the appendix I). Hence, we took the first difference of  $p_6$ ,  $p_8$  and  $p_{12}$ , and named them as  $dp_6$ ,  $dp_8$  and  $dp_{12}$ , respectively.

Tables A.8 to A.11 in the appendix I show the results of the four estimated VARs<sup>10</sup>. For the four-month window VAR, only the lagged terms of each variable are significant and, differently from the previous case, the volatility of IPCA would not affect the exchange rate volatility. As for the six-month window, contrary to what was observed in the standard deviation case, the only significant terms are the dummy and the first lag of the exchange rate volatility in its own equation. In the eight-month window, we do not find the correlation problem we found before but, again, the only term that is significant is  $e6(-1)$  in the equation for the exchange rate variance. Finally, the VAR between  $dp12$  and  $e12$  indicates  $e12(-1)$  as the only significant variable in the equation for  $e12$ . In the equation for inflation variance, the coefficients for  $e12(-1)$  and  $e12(-2)$  are significant and the Wald test shows that their sum is statistically different from zero at a 10% level.

Graph 4 – Variances of IPCA (variances) – Rolling Windows



Graph 5 – Variances of E (variances) – Rolling Windows



In sum, we notice that the results differ from the ones obtained in the case with standard deviations concerning unit root tests, the number of lags in the VAR and the significance of some variances. None of the models showed that inflation volatility is affected by its lagged term, differently from what happens to exchange rate volatility. When it comes to cross-terms, we find that exchange rate volatility is significant in explaining inflation volatility in the 12-month windows. Hence, one can realize that results are sensitive not only to window size but also to the method chosen to compute volatility. In addition, since there are lagged effects in the case of exchange rate variance, we reinforce the adequacy of investigating a GARCH-type model.

<sup>10</sup> .D2002\_M11 was included for the six-month window case

### 4.3. Variance decomposition in a VAR model

The last exercise performed in this section was to test a VAR between the price index and the exchange rate and to analyze variance decomposition. Since both series have unit roots, as shown in Table 1, we first tested for the presence of cointegration vectors. As shown in Table A.12 in the appendix I, the Trace and Eigenvalue tests do not accept the null hypothesis of presence of a cointegration vector.<sup>11</sup> For this reason, we will test a VAR between the first differences of price index (IPCA) and exchange rates (E).

In the variance decomposition factorization by Cholesky method, we chose E preceding IPCA, since we consider the former to be more exogenous than the latter. The Granger test may be used to give further support in the ordering decision (table A.13 in the appendix I. However, since the correlation between the residuals is low ( $-0.17 < |0.20|$ )<sup>12</sup> the order does not have significant effects over the results. Table A.14 shows the VAR results, while Table A.15 presents the variance decomposition.

By analyzing the variance decomposition in table A.15, we find that about 3% of the movements in IPCA in  $t+1$  may be explained by shocks in E in period  $t$ . There are increasing accumulated effects over time, and shocks in E explain around 42% of the movements in IPCA after 12 months. A shock in IPCA, in its turn, does not have an immediate effect on the sequence of E, however it has lagged effects, although on a smaller scale.

Graphs 6 to 9 show these decompositions over time, as well as the interval of  $\pm 2$  standard errors. We notice that shocks to the variables have positive effects on their sequences, and apart from the impact of IPCA on E, they are different from zero. Therefore, we cannot rule out the hypothesis that shocks to the exchange rate – represented by  $\eta_t$  in equation (3) – might affect inflation.

Based on the results presented in this section, we may infer that the traditional measures used to verify whether there is a relation between the volatilities of exchange rate and macroeconomic variables (standard deviations or variances in subsamples) yield results that are sensitive to the subsample size, leading us to accept or reject the significance of the relation according to the window size we are working with.

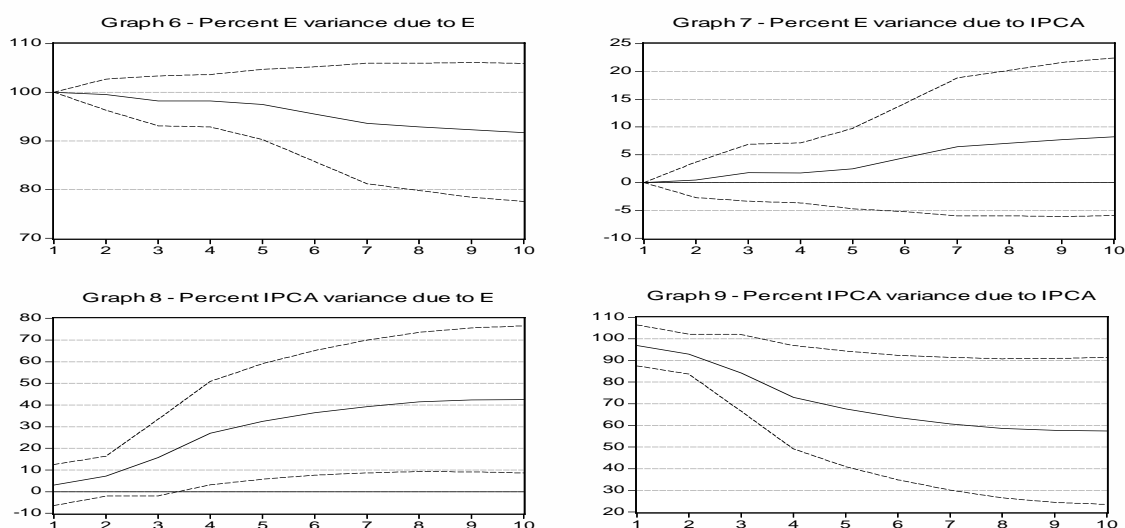
The variance decomposition, in its turn, indicates that shocks to the exchange rate affect inflation variance. Since volatility is also a measure of uncertainty, this result sounds more intuitive than some of those presented before: if the exchange rate affects inflation and has

---

<sup>11</sup> The conclusion is the same if we consider only one lag.

<sup>12</sup> Enders (1995) suggests, as a rule-of-thumb, that a correlation between residuals of the variables  $< |0.2|$  is not strong enough to affect the results in the Cholesky decomposition.

delayed effects (incomplete exchange rate pass-through in the short run), shocks to that variable will affect the uncertainty about future inflation. Besides, an adequate exchange rate model must consider the presence of conditional heteroskedasticity, as illustrated in Table A.16 in the appendix. In this case, it is necessary to generate volatility series for both variables in the same way - hence, to consider conditional variance for both - and not simply compare the variance series obtained from a GARCH (p,q) model for the exchange rates with an exogenous measure of inflation volatility. Furthermore, we show that variance decomposition reports that shocks to the IPCA affect its variance, just as well as some of the results obtained in the rolling window procedure show us that IPCA volatility is affected by its past values, reinforcing the application of the test for a bivariate GARCH model with E and IPCA.



## 5. Tests with conditional variance– Bivariate GARCH

Testing a GARCH model requires, first, some assumption about the mean equations. We considered, therefore, three different cases. The first one is consisted of only lagged terms of each variable; the second, of a Phillips Curve for the IPCA equation (according to equation 2 in Section 2) and the lagged values for the exchange rate; the third, of the Phillips Curve for the IPCA and a random walk with drift for the exchange rate (equation 3 in Section 2). According to unit root tests previously performed, both variables were considered in first differences of their logarithms. Considering both the cross-correlograms and OLS models, we chose the number of lags in the equations for IPCA and exchange rate.<sup>13</sup> With regard to variance specifications, we

<sup>13</sup> When they pointed to different number of lags, we tested the highest one.

tested five different options: diagonal-Vec (Bollerslev, Engle and Wooldridge, 1988), constant correlation (CCORR, from Bollerslev, 1990), full parameterization (Vec), the BEKK restriction (Engle and Kroner, 1993) and the dynamic conditional correlation (DCC, from Engle, 2000). Only under the BEKK restriction convergence was achieved, and we consider some reasons for that further ahead in this section.

The general form of mean, variance and covariance equations under the BEKK model are:

Mean equations

$$IPCA = \delta_0 + \delta_1 IPCA_{t-1} + \delta_2 E_{t-1} + \delta_3 E_{t-2} + \delta_4 GAP_{t-2} + \delta_5 PPI_{t-1} + \varepsilon_{1,t}$$

$$E = \gamma_0 + \gamma_1 E_{t-1} + \gamma_2 E_{t-2} + \varepsilon_{2,t}$$

Variance and Covariance equations<sup>14</sup>

$$h_{11} = c_{11} + a_{11}^2 \varepsilon_{1,t-1}^2 + 2a_{11}a_{21} \varepsilon_{1,t-1} \varepsilon_{2,t-1} + a_{21}^2 \varepsilon_{2,t-1}^2 + g_{11}^2 h_{11,t-1} + 2g_{11}g_{21} h_{12,t-1} + g_{21}^2 h_{22,t-1}$$

$$h_{22} = c_{22} + a_{12}^2 \varepsilon_{1,t-1}^2 + 2a_{12}a_{22} \varepsilon_{1,t-1} \varepsilon_{2,t-1} + a_{22}^2 \varepsilon_{2,t-1}^2 + g_{12}^2 h_{11,t-1} + 2g_{12}g_{22} h_{12,t-1} + g_{22}^2 h_{22,t-1}$$

$$h_{12} = c_{21} + a_{11}a_{12} \varepsilon_{1,t-1}^2 + (a_{12}a_{22} + a_{21}a_{12}) \varepsilon_{1,t-1} \varepsilon_{2,t-1} + a_{21}a_{22} \varepsilon_{2,t-1}^2 + g_{12}g_{11} h_{11,t-1} + (g_{11}g_{22} + g_{12}g_{21}) h_{12,t-1} + g_{21}g_{22} h_{22,t-1}$$

In order to make the analysis clearer, we renamed the coefficients above as:

$$c_{11} = \alpha_0; a_{11}^2 = \alpha_1; 2a_{11}a_{21} = \alpha_2; a_{21}^2 = \alpha_3; g_{11}^2 = \alpha_4; 2g_{11}g_{21} = \alpha_5; g_{21}^2 = \alpha_6$$

$$c_{22} = \beta_0; a_{12}^2 = \beta_1; 2a_{12}a_{22} = \beta_2; a_{22}^2 = \beta_3; g_{12}^2 = \beta_4; 2g_{12}g_{22} = \beta_5; g_{22}^2 = \beta_6$$

$$c_{21} = \mu_0; a_{11}a_{12} = \mu_1; a_{12}a_{22} + a_{21}a_{12} = \mu_2; a_{21}a_{22} = \mu_3; g_{12}g_{11} = \mu_4; g_{11}g_{22} + g_{12}g_{21} = \mu_5; g_{21}g_{22} = \mu_6$$

Hence, the variance and covariance equations can be rewritten as:

$$h_{11} = \alpha_0 + \alpha_1 \varepsilon_{1,t-1}^2 + \alpha_2 \varepsilon_{1,t-1} \varepsilon_{2,t-1} + \alpha_3 \varepsilon_{2,t-1}^2 + \alpha_4 h_{11,t-1} + \alpha_5 h_{12,t-1} + \alpha_6 h_{22,t-1}$$

$$h_{22} = \beta_0 + \beta_1 \varepsilon_{1,t-1}^2 + \beta_2 \varepsilon_{1,t-1} \varepsilon_{2,t-1} + \beta_3 \varepsilon_{2,t-1}^2 + \beta_4 h_{11,t-1} + \beta_5 h_{12,t-1} + \beta_6 h_{22,t-1}$$

$$h_{12} = \mu_0 + \mu_1 \varepsilon_{1,t-1}^2 + \mu_2 \varepsilon_{1,t-1} \varepsilon_{2,t-1} + \mu_3 \varepsilon_{2,t-1}^2 + \mu_4 h_{11,t-1} + \mu_5 h_{12,t-1} + \mu_6 h_{22,t-1}$$

For each case, different simulations were made changing the convergence criteria and the number of iterations. Therefore, it is possible that, for each case, we ended up with more than one result achieving convergence. When this occurred, the choice was made based on the following criteria: LM and the ARCH-LM tests (i.e. absence of residual serial correlation and of arch-type residuals), calculation of the eigenvalues to assure that the condition of covariance stationarity was respected (see Engle and Kroner, 1993 for further details on conditions and tests), and, when all the previous were respected, we chose the result that maximized, for the case considered, the likelihood function. The final results are presented in table 2.

<sup>14</sup> Variance and covariance equations are from Engle and Kroner (1993), equation 2.3, pages 5 and 6, without suppressing the GARCH terms.

**Table 2 – Bivariate GARCH Results**

Monthly data from 1999:01 to 2004:09

	Variables	Case 1	Case 2	Case 3 <sup>a</sup>
<b>Function Value</b>		548.5888337	558.7008734	548.0509755
<b>Equation for IPCA</b>	Constant	0.00282329* (0.0005596)	0.00197323* (0.00050458)	0.0011409* (0.00051313)
	IPCA <sub>t-1</sub>	0.55715402* (0.07376155)	0.57849083* (0.0609667)	0.68315183* (0.05967424)
	E <sub>t-1</sub>	-	0.03863824* (0.00980401)	0.06380358* (0.00779833)
	E <sub>t-2</sub>	-	-0.00073484 (0.00964137)	-0.00920641 (0.0073217)
	GAP <sub>t-2</sub>	-	0.01673604** (0.00977043)	0.01552899** (0.0095768)
	PPI <sub>t-1</sub>	-	0.09498593** (0.05367548)	0.10285839* (0.05499651)
<b>Equation for E</b>	Constant	0.00669639 (0.00424251)	0.01229489* (0.0043067)	0.01917512* (0.00534423)
	E <sub>t-1</sub>	0.8094822* (0.11426506)	0.60752556* (0.12549928)	-
	E <sub>t-2</sub>	-0.22750191** (0.13597143)	-0.16772685 (0.10694474)	-
<b>Conditional variance of IPCA</b>	$\alpha_0$	0	0	0
	$\alpha_1$	+	+	+
	$\alpha_2$	+	+	+
	$\alpha_3$	+	+	+
	$\alpha_4$	0	0	0
	$\alpha_5$	0	0	0
	$\alpha_6$	0	0	0
<b>Conditional variance of E</b>	$\beta_0$	0	0	0
	$\beta_1$	+	0	+
	$\beta_2$	+	0	+
	$\beta_3$	+	+	+
	$\beta_4$	+	+	+
	$\beta_5$	+	+	+
	$\beta_6$	+	+	+
<b>Covariance</b>	$\mu_0$	+	+	-
	$\mu_1$	-	0	-
	$\mu_2$	-	-	-
	$\mu_3$	-	-	-
	$\mu_4$	0	0	0
	$\mu_5$	0	0	0
	$\mu_6$	0	0	0

Notes: (a) case presents residual autocorrelation in both mean equations (LM test); residuals of ARCH-type in the exchange rate equation; standard deviations in parentheses; \* and \*\* denote significance at 5% and 10%, respectively.

By analyzing Table 2, we notice that the results for the mean equations are quite similar, as well as the values in the variance equation for cases (1) and (2). Case (3) differs from the



other two but, since that model has ARCH residuals for the equation of E and serial correlation of residuals for both mean equations<sup>15</sup>, it cannot be considered as a good model.

Comparing the variance equations in cases (1) and (2), we see that the differences lie in the signs of  $g_{12}$  and  $g_{22}$ , in the values of  $a_{11}$ ,  $a_{22}$  and  $a_{12}$  and in the significance of coefficients  $\mu_1$ ,  $\beta_1$  and  $\beta_2$ , that is, the impact of  $\varepsilon_{1,t-1}^2$  on the conditional variance of E (first difference of the exchange rate) and in the covariance and impact of  $\varepsilon_{1,t-1}^2 \varepsilon_{2,t-1}^2$  on the conditional covariance of E.

However, it can be seen from Table 3 that the significance of  $\mu_1$ ,  $\beta_1$  and  $\beta_2$  is the only significant difference between both cases. The difference in the signs of  $g_{12}$  and  $g_{22}$  does not affect the final result because these coefficients are considered under three situations: (i) squared values; (ii) multiplied by each other, (iii) multiplied by coefficients that are statistically equal to zero. The differences in  $a_{11}$ ,  $a_{22}$  and  $a_{12}$ , in their turn, fall within standard deviation boundaries, thus, they may not be considered to be significant. It is important to notice that for the inflation equation all cases provided the same signals and the same significance (i.e. if statistically equal to or different from zero). Therefore, our results for the response of IPCA to shocks in E are robust.

The Wald Test was performed to decide between the cases considered. The unrestricted case – that is, case (2) – was preferred to the detriment of cases (1) and (3), as shown in Table 4. Hence, we will consider case (2) as our results from now on.

Tables 5 to 8 show the results of the Ljung-Box and LM tests for auto-correlation of residuals, the Arch-LM test for Arch-type residuals, the multivariate Portmanteau test for cross-correlation and the eigenvalue vector<sup>16</sup> for case 2. As it can be seen from these tables, the model estimated in case 2 respects the conditions of no serial autocorrelation or cross-correlation of residuals, no Arch-type residuals and is covariance stationary. Therefore, we can say that the dependence between exchange rate and inflation volatilities was completely captured by the bivariate-Garch model.

By analyzing the results of case 2, shown in the second column of Table 2, one can notice that the conditional variance of IPCA is affected (statistically significant) by shocks to the IPCA, E and shocks common to both. However, since  $\alpha_1$  and  $\alpha_3$  are square coefficients, we cannot determine whether the effects of IPCA and E shocks have a positive or negative sign, but we can

---

<sup>15</sup> We could not find any model that removed the autocorrelation in the mean equation of the exchange rate, which was expected since there are no lagged terms in that equation.

<sup>16</sup> For a brief explanation of the eigenvalue calculation, see Appendix II.

affirm that they are statistically significant. Lagged variances and covariances, however, do not play a significant role in explaining IPCA variance.

As for the conditional variance of E, it is affected by its lagged values and by lagged values of the conditional variance of IPCA – the latter goes undetected by almost all tests with unconditional variances – although we also cannot make assertions about the sign. Shocks common to both variables ( $\varepsilon_{1,t-1}\varepsilon_{2,t-1}$ ) and in the covariance have a positive and significant sign. Graph 10 shows the estimated conditional variances over time.

**Table 3 - Estimated Parameters in Variance and Covariance Equations**

Monthly data from 1999:01 to 2004:09

G <sub>11</sub>	-0.1041899 (0.1348117)	-0.0513807 (0.11993625)	0.03980506* (0.14292026)
g <sub>21</sub>	0.00810385 (0.01683404)	0.01085598 (0.01418979)	-0.00743866* (0.0156595)
g <sub>12</sub>	12.52650218* (1.55221793)	-13.00132891* (1.68386503)	13.12325566* (1.98208477)
g <sub>22</sub>	0.41076103** (0.23448881)	-0.43513845* (0.21248228)	0.50120845* (0.22752382)
a <sub>11</sub>	0.27491257* (0.12289452)	0.40438372* (0.13130784)	-0.44434782* (0.17146475)
a <sub>21</sub>	0.0595035* (0.0131604)	0.05305404* (0.01178906)	-0.05393149* (0.01283429)
a <sub>12</sub>	-3.42461647** (1.98123913)	-5.71185332* (2.10969805)	7.4208698 (2.41134849)
a <sub>22</sub>	-0.46199166* (0.1406473)	-0.59176609* (0.14044079)	0.78655762* (0.16694871)
c <sub>11</sub>	-0.00000016 (0.007226)	-0.00000008 (0.00455714)	0.00000006 (0.00519676)
c <sub>21</sub>	0.00211834* (0.00037541)	0.00175652* (0.00033542)	-0.00189984* (0.00031271)
c <sub>22</sub>	0.00366595 (0.00836578)	0.0038599 (0.00918004)	-0.00462995 (0.01001528)
	(0.00836578)	(0.00918004)	(0.01001528)

**Table 4 –Wald Test<sup>17</sup>**

Cases tested	Observed $\chi^2_q$ statistic	Null hypothesis: Variables added in case (2) are not jointly significant
Case (1) vs Case (2)	20.22	Reject
Case (2) vs. Case (3)	21.30	Reject

<sup>17</sup> Wald Test:  $-2(l_r - l_u) \sim \chi^2_q$ , where q is the number of added variables,  $l_r$  and  $l_u$  are the log-likelihood of the restricted and unrestricted cases, respectively. Under  $H_0$ , the added variables are not jointly significant.

**Table 5 –Ljung-Box Tests for Residual Autocorrelation**

Ljung-Box	E1 (residuals of inflation Equation)		E2 (residuals of exchange rate equation)	
	Q-Statistics	Significance Level	Q-Statistics	Significance Level
Q(1-0)	0.0041	0.9491	0.0934	0.7599
Q(2-0)	0.8666	0.6484	0.1501	0.9277
Q(3-0)	1.4555	0.6926	0.1737	0.9817
Q(4-0)	1.8807	0.7577	1.2716	0.8662
Q(5-0)	1.9857	0.8511	1.7955	0.8766
Q(6-0)	3.2571	0.7760	2.3153	0.8885
Q(7-0)	3.6674	0.8172	2.9063	0.8935
Q(8-0)	6.2370	0.6207	6.2032	0.6245
Q(9-0)	6.5844	0.6803	6.3149	0.7080
Q(10-0)	6.8781	0.7369	7.5265	0.6750
Q(11-0)	7.5425	0.7536	12.2845	0.3426
Q(12-0)	13.8282	0.3118	12.9173	0.3751

**Table 6 – LM and ARCH-LM Tests**

Lags	Qui-square critical level at 5%	N*R2 values <sup>18</sup>			
		Inflation Equation		Exchange Rate Equation	
		LM test	Arch-LM test	LM test	Arch-LM test
1	3.8415	1.1927	0.9080	3.3525	0.4656
2	5.9915	4.9930	2.1524	4.1045	3.0632
3	7.8147	5.5838	6.5384	2.7580	3.3708
4	9.4877	6.2760	7.8664	5.3360	3.6771
5	11.0705	7.8937	8.0904	7.2583	3.4554
6	12.5916	8.5463	8.9747	9.3236	4.2765
7	14.0671	12.1124	8.9349	13.0569	4.7729
8	15.5073	14.6820	9.1488	18.5930	4.9308
9	16.9190	14.9107	9.5050	18.1027	5.4148
10	18.3070	14.8134	9.9457	18.3225	5.3254
11	19.6751	15.1475	11.3772	20.7173	5.7317
12	21.0261	19.7229	9.7259	20.2341	10.0397

**Table 7– Multivariate Portmanteau Test for Cross-Correlation<sup>19</sup>**

M	Test Statistics	Significance Level
3	5.6954	0.3370
5	12.2948	0.5036
7	16.5348	0.7389
10	25.0132	0.8394
12	36.2776	0.6803
15	45.2643	0.7660

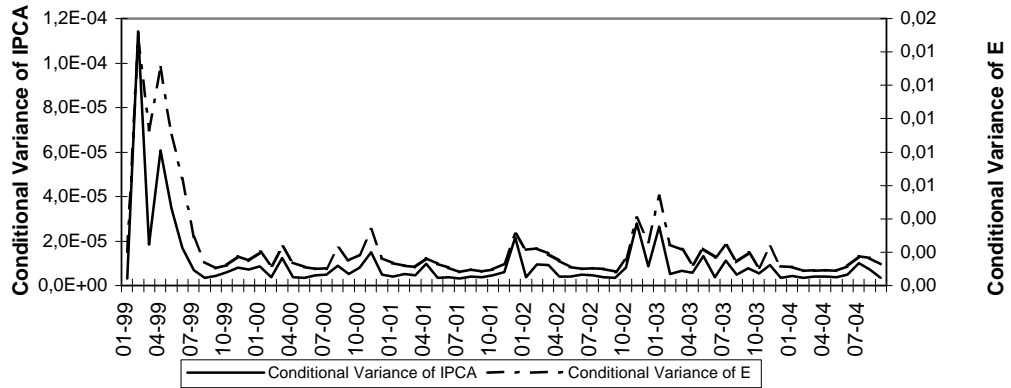
<sup>18</sup> The N\*R2 value must be < than the  $\chi^2$  to accept the null hypotheses of no autocorrelation and arch residuals.

<sup>19</sup>  $H_0: \rho_1 = \rho_2 = \dots = \rho_m = 0$  and  $H_a: \rho_i \neq 0$  for some  $i \in \{1, \dots, m\}$  (See TSAY, 2002, for the multivariate Portmanteau test for cross-correlation).

**Table 8 – Eigenvalue Vector**

$$y = \begin{bmatrix} 0.6630 \\ -0.4252 \\ -0.0770 \\ 0.0637 \end{bmatrix}$$

**Graph 10 – Conditional Variances - IPCA and E**



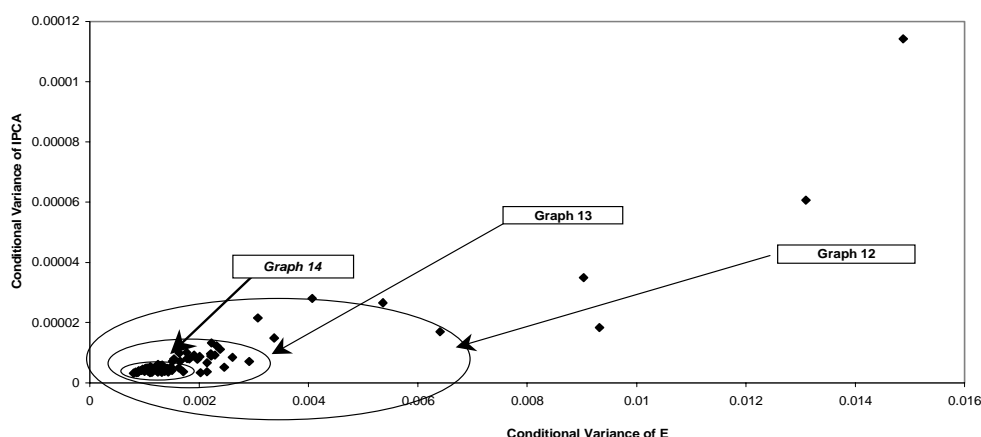
Finally, results show us that shocks in the exchange rate (E) and shocks common to exchange rate and IPCA have negative and significant effects over the covariance between the two variables. This is an important result in our model. It means that shocks that affect the exchange rate or the exchange rate and IPCA simultaneously will cause a “disconnection” of these two variables. After all, everything else the same, a reduction in the covariance means a reduction in the correlation coefficient between the variables.

At first, we considered that the lack of convergence for specifications other than the BEKK model would result from the small size of our sample (January, 1999 to September, 2004). However, this may be questioned since the BEKK specification has more parameters than some of the other specifications tested. The negative sign of shocks in E over the conditional covariance ( $\mu_1 < 0$ ) and the dispersion graphs presented below (graphs 11 to 14) suggest that the sign of shocks in E over the conditional variance of IPCA may not be the same all the time. If this is true, then we may have a reason for the non-convergence of specifications that, instead of working with squared terms (imposing the positivity of the matrix), try to find a sign for the relation. In these specifications, if the signs of a coefficient in the equations of exchange rate’s and inflation’s variances change from positive to negative, they will not converge to a final value, since the model will have to establish whether the coefficient is positive or negative. In

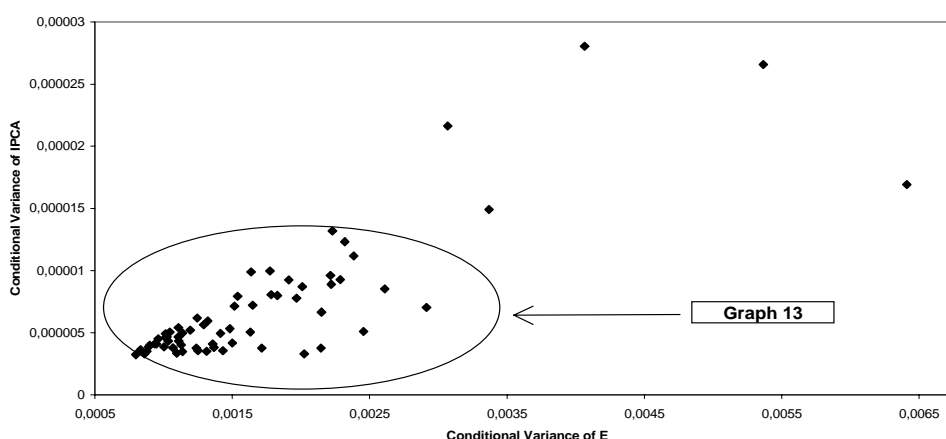
the BEKK specification, however, this problem does not exist once it works with square coefficients. However, further tests are necessary before we can make such assertion.

Graphs 11 to 14 are dispersion graphs with the conditional variances of E on the horizontal axis and of IPCA on the vertical axis. Graph 11 plots the entire sample and one can clearly see four outliers in that graph, which correspond to the period between February and May 1999 (i.e. the first months after the change in the exchange rate regime, caused by the 1999 crisis, and before the adoption of the inflation-targeting regime in June of that year). Hence, we excluded these observations and built Graph 12. Again, five outliers were removed to construct Graph 13 (June 1999, November 2000, December 2001, December 2002 and January 2003). Graph 14, in its turn, was built using only the region with the highest concentration of observations (57% of the sample).<sup>20</sup>

**Graph 11 — Exchange rate and inflation volatilities (full sample)**

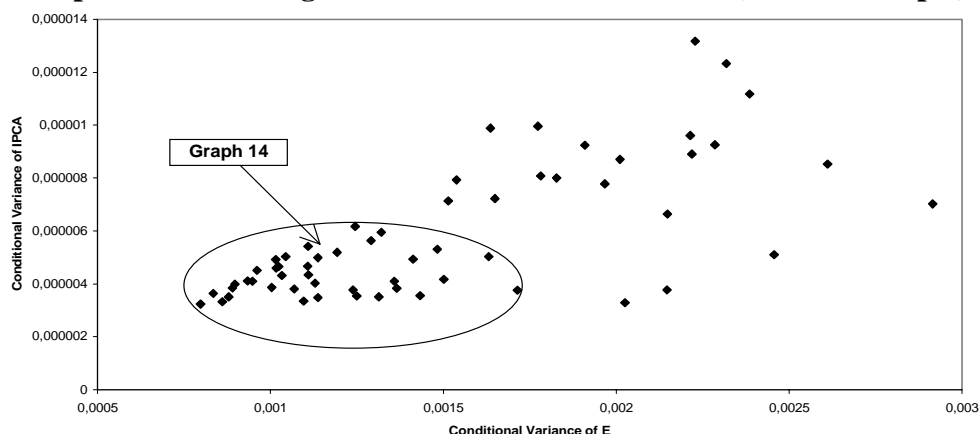


**Graph 12 — Exchange rate and inflation volatilities (reduced sample)**

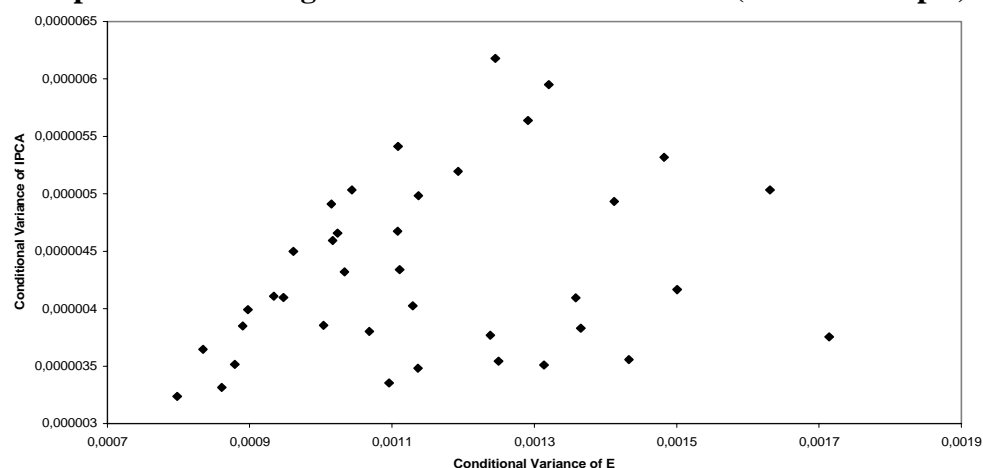


<sup>20</sup>The observations removed from Graph 14 are, related to Graph 11: January to July 1999; November 1999 to January 2000; March, August, October and November 2000; April 2001; December 2001 to March 2002; October 2002 to March 2003; May, July, September and November 2003 and August 2004.

**Graph 13 — Exchange rate and inflation volatilities (reduced sample)**



**Graph 14 — Exchange rate and inflation volatilities (reduced sample)**



Graph 12 and, mainly, graph 13 suggest a semiconcave (if not concave) relation between the two variables at stake (i.e. the conditional variances of exchange rate and of IPCA). To illustrate the relation, a trend was included in those graphs and in graph 14, and the adjusted  $R^2$  of each trend equation was reported (see graphs A.1 to A.3 in the appendix I). The semiconcave relation would imply that, although the response of inflation volatility to exchange rate volatility is positive, the proportion in its variation decreases as exchange rate volatility rises.

If we consider graph 14, which plots the region with the highest concentration of observations, we find a clear concave relation. This would mean that, after a certain point, the positive relation between volatilities becomes negative, as opposed to the convex form observed in financial variables (the so-called *smile of volatility*). Also, it is possible that it is reflecting the existence of a regime switching in the volatilities, since we are removing the extreme values of the sample. We need a longer sample to test if this behavior would be reproduced over time. However, we can only use graph 14 to speculate about these possibilities happening.

Nonetheless, it is a question to be answered in future research, since some works of other authors find, as we pointed out in the introduction, the sign may change according to the model's parameters.

## 6. Conclusions

The analysis presented in sections 4 and 5 show that the use of unconditional variances leads us to results that are sensitive to the chosen measure of volatility, which is based on subjective criteria. The multivariate GARCH model, dealing directly with the effects of conditional volatilities, finds a semi-concave relation (differently from the case for financial series, where this relation has a convex form), statistically significant, between exchange rate and inflation variances.

The results seem to be in line with the intuition obtained from other studies, especially Dixit (1989) and Seabra (1996). When exchange rate volatility is very high, increasing uncertainty, inflation response may be reduced, leading to smaller effects. This may explain why some studies to Brazil found a decrease in the short-run pass-through from exchange rates to consumer prices after the floating regime.

The analysis based on the role played by uncertainty could also make a bridge between the two different points of view concerning the existence of a relation between the volatilities of exchange rate and inflation. The relation would exist but, under certain conditions, the disconnection between the variables would be too strong to be noticed. In periods of high volatility, agents will not respond with the same intensity as they do in periods of stability due to the lack of knowledge concerning the duration of the movements in the exchange rate (whether temporary or permanent). Therefore, inflation volatility has smaller amplitude. On the other hand, when exchange rate volatility is lower, inflation would respond more promptly<sup>21</sup>. This disconnection becomes clearer in the negative sign found in the response of the conditional covariance to shocks in the exchange rate and would be reinforced if the sign reversion found in graph 14 is verified in future studies.

The caveats of this paper basically lie in the small sample available for Brazil, since the floating regime for exchange rates having started only in 1999. Because of that, we cannot establish with certainty whether the problems faced with convergence were due to the sign

---

<sup>21</sup> For instance, in an environment with fixed exchange rates, the agents know that devaluation is permanent. Therefore, facing a new level of the exchange rates, they need to adjust their costs. The same is not true under a floating system: agents have costs to adjust their prices to a new level of exchange rates and costs to return to the original position if the (de)valuation is not permanent.

instability or to the small period involved. Nonetheless, we tend not to rely too much in the small sample explanation, since three out of the other four restrictions tested – diagonal VEC, CCORR and DCC – have less parameters to be estimated. Nonetheless, a large sample is essential to corroborate the results.

However, this article innovates by (i) applying a multivariate GARCH model, thus, considering conditional variances to analyze the relation between volatilities, (ii) trying to establish a relation between exchange rate and inflation volatilities and its possible implications for monetary policy and (iii) showing that traditional tests performed with exogenously constructed volatility series are sensitive to the criteria chosen to construct such series and do not reveal relevant features of that relation.



## References

- Andersen, T. M. (1997) "Exchange rate volatility, nominal rigidities and persistent deviations from PPP", *Journal of the Japanese and International Economies*, 11, pp. 584-609
- Barkoulas, J. T.; Baum, C.F.; Caglayan, M. (2002) "Exchange rate effects on the volume and variability of trade flows", *Journal of International Money and Finance*, 21, pp. 481 – 496
- Barone-Adesi, G.; Yeung, B. (1990) "Price flexibility and output volatility: the case for flexible exchange rate", *Journal of International Money and Finance*, 9, pp. 276 – 298
- Barro, R.J., Gordon, D.B. (1983) "Rules, discretion, and reputation in a model of monetary policy", *Journal of Monetary Economics*, 12, 101-120
- Bastourre, Diego; Carrera, Jorge (2004) "Could the Exchange Rate Regime Reduce Macroeconomic Volatility?" In: *Latin American Meeting Of The Econometric Society (LAMES)*, Santiago, 27-30, July, *Analls...*, CD-ROM
- Baxter, M.; Stockman, A.C. (1988) "Business cycle and the exchange rate system: some international evidence", *NBER*, working paper no. 2689, August
- Bleaney, M. (1996) "Macroeconomic stability, investment and growth in developing countries", *Journal of development economics*, vol. 48, pp. 461-477
- Bleaney, M.; Fielding, D. (2002) "Exchange rate regimes, inflation and output volatility in developing countries", *Journal of Development Economics*, v. 68, pp. 233-245
- Bollerslev T., Engle, R. F. and Wooldridge, J. M. (1988) "A Capital Asset Pricing Model with Time-varying Covariances", *Journal of Political Economy*, v. 96, no. 1
- Bollerslev, Tim (1990), "Modelling the coherence in short-run nominal exchange rates", *Review of Economics and Statistics*, 72, pp. 498–505.
- Calvo, G.; Reinhart, C. (2000a) "Fear of Floating", *NBER*, working paper no. 7993, November
- Calvo, G.; Reinhart, C. (2000b) "Fixing for your life", *NBER*, working paper no. 8006, November
- Chen, N. (2004) "The behaviour of relative prices in the European Union: A sectoral analysis", *European Economic Review*, 48, pp. 1257-1286
- Devereux, M. B.; Engel, C. (2003) "Monetary Policy in the Open Economy Revisited: Price Setting and Exchange Rate Flexibility", *The Review of Economic Studies*, October
- Dixit, A. (1989) "Hysteresis, import penetration, and exchange rate pass-through", *The Quarterly Journal of Economics*, CIV, May, pp. 205-228
- Duarte, M.; Stockman, A.C. (2002) "Comment on: Exchange rate pass-through, exchange rate volatility, and exchange rate disconnect", *Journal of Monetary Economics*, v. 49, n. 5, July, 941-946
- Enders, W. (1995) *Applied econometric time serie*, John Wiley & Sons, Nova York
- Engel, C.; Rogers, J. H. (2001) "Deviations from purchasing power parity: causes and welfare costs", *Journal of International Economics*, 55, pp. 29-57
- Engle, Robert F. (2002) "Dynamic conditional correlation – a simple class of multivariate GARCH models", *Journal of Business and Economic Statistics*, v.20, n.3, July
- Engle, R.F.; Kroner, K. F. (1993) "Multivariate Simultaneous Generalized ARCH", *University of California, San Diego*, discussion paper 89-57R, June

- Flood, R.P.; Rose, A. K. (1995) “Fixing exchange rates – a virtual quest for fundamentals”, *Journal of Monetary Economics*, 36, pp. 3 – 37
- Ghosh, A. R.; Gulde, A.M.; Ostry, J. D.; Holger, C. W. (1997) “Does the nominal exchange rate regime matter?” *NBER*, working paper no. 5874, January
- Hamilton, J. D. (1994) *Time series Analysis*, Prentice Hall, London
- Hausmann, R.; Panizza, U.; Stein, E. (2001) “Why do countries float the way they float?” *Journal of Development Economics*, vol. 66, pp. 387 – 414
- Krugman, P. (1988); “*Exchange Rate Instability*”, Cambridge, MA: The MIT press
- Obstfeld, M; Rogoff, K. (2000) “The six major puzzles in international macroeconomics: is there a common cause?” *NBER*, working paper no. 7777, July
- Rogoff, K. (2001) “Perspectives on exchange rate volatility” in: Feldstein, M. (ed), *International Capital Flows*, Chicago: University of Chicago Press, 441 - 453
- Seabra, F. (1996) “A relação teórica entre incerteza cambial e investimento: os modelos neoclássico e de investimento irreversível”, *Política e Planejamento Econômico*, v. 26, n. 2, pp. 183 – 202, August
- Smith, C. E. (1999) “Exchange rate variation, commodity price variation and the implications for international trade”, *Journal of International Money and Finance*, 18, pp, 471– 491
- Sutherland, A. (2002) “Incomplete pass-through and the welfare effects of exchange rate variability”, *CEPR*, Discussion Paper No 3431
- Tsay, Ruey S. (2002) *Analysis of Financial Time Series*, John Wiley & Sons, Inc
- Wei, S.; Parsley, D. (1995) “Purchasing power disparity during the floating rate period: exchange rate volatility, trade barriers and other culprits”, *NBER*, working paper no. 5032, February

## Appendix I – Tables & Graphs

Table A.1 – ADF Unit Root Test

<i>sample: 2000:03 to 2004:10</i>				
Variable	ADF test statistics	Critical value at 5%	ADF test statistics –first difference of the variable	Critical value at 5%
Price Index	-2.1704 <sup>(a)</sup>	-3.4783	-3.904127 <sup>(a)</sup>	-3.4783
Exchange Rate	-1.7097 <sup>(a)</sup>	-3.4783	-7.427513 <sup>(a)</sup>	-3.4783
External Prices	-1.5419 <sup>(a)</sup>	-3.4783	-8.014687 <sup>(a)</sup>	-3.4793
GAP	-9.7018	-2.9077	-	-

Note: test performed with (a) trend or intercept and (b) without trend.

Table A.2 – ADF Unit Root Test – std. dev.

<i>sample: 2000:03 to 2004:10</i>				
Variable	ADF test statistics	Critical Value at 5%	ADF test statistics – first difference of variables	Critical Value at 5%
IPCA_4	-3.4697	-3.4805	-	-
IPCA_6	-1.8540 <sup>(a)</sup>	-1.9461	-	-
IPCA_8	-1.3046 <sup>(a)</sup>	-1.9463	-7.0015	-3.4865
IPCA_12	-0.8823 <sup>(a)</sup>	-1.9465	-5.9875	-3.4921
E_4	-11.9597	-3.4816	-	-
E_6	-10.8574 <sup>(b)</sup>	-2.9084	-	-
E_8	-9.5054 <sup>(b)</sup>	-2.9100	-	-
E_12	-7.5521 <sup>(b)</sup>	-2.9136	-	-

Note: test performed with (a) trend or intercept and (b) without trend.

Table A.3 – VAR for four-month windows

Variables	E_4	IPCA_4	Variables	E_4	IPCA_4
E_4(-1)	0.2790 (0.0449) [ 6.2085]	-5.65E-05 (0.0004) [ -0.1423]	D2002_M11	0.005 (0.001) [ 5.1319]	7.11E-05 (8.7E-06) [ 8.1232]
IPCA_4(-1)	21.8600 (7.7321) [ 2.8272]	0.7206 (0.0683) [ 10.5446]	D1999	0.0121 (0.0015) [ 7.8898]	1.59E-06 (1.4E-05) [ 0.1177]
C	0.0004 (0.0002) [ 2.2992]	2.27E-06 (1.4E-06) [ 1.5965]	R-squared	0.8856	0.7384
			Adj. R-squared	0.8779	0.7210
			F-statistic	116.0581	42.3377

Note: standard deviations between parentheses; t-statistics in brackets.

Table A.4 – VAR for six-month windows

Variables	E_6	IPCA_6	Variables	E_6	IPCA_6	Variables	E_6	IPCA_6
E_6(-1)	0.9027 (0.1118) [ 8.0747]	0.0034 (0.0018) [ 1.9157]	E_6(-6)	0.0706 (0.0482) [ 1.4657]	-0.0010 (0.0008) [-1.343]	IPCA_6(-5)	-26.5070 (7.8289) [-3.3858]	-0.0059 (0.1248) [-0.0469]
E_6(-2)	0.0398 (0.1483) [ 0.2684]	-0.0064 (0.0024) [-2.7097]	IPCA_6(-1)	0.4882 (7.085) [ 0.0689]	0.8246 (0.1129) [ 7.3032]	IPCA_6(-6)	19.6540 (6.1560) [ 3.1927]	-0.0141 (0.0981) [-0.1434]
E_6(-3)	0.0239 (0.1548) [ 0.1546]	-0.0002 (0.0025) [-0.0727]	IPCA_6(-2)	1.8361 (9.0902) [ 0.202]	0.1457 (0.1449) [ 1.0061]	C	0.0002 (0.0001) [ 1.8206]	1.86E-06 (1.8E-06) [ 1.0462]
E_6(-4)	-0.1345 (0.1139) [-1.1809]	0.0043 (0.0018) [ 2.3814]	IPCA_6(-3)	-4.3719 (8.7652) [-0.4989]	-0.0721 (0.1397) [-0.5159]	D2002_M11	0.0028 (0.0004) [ 6.5062]	4.59E-05 (6.8E-06) [ 6.7698]
E_6(-5)	-0.1018 (0.0874) [-1.1643]	0.0005 (0.0019) [ 0.3891]	IPCA_6(-4)	7.9487 (8.6463) [ 0.9193]	-0.0954 (0.1378) [-0.6920]	R-squared F-statistic Adj. R-squared	0.88102 25.0626 0.8459	0.8588 20.5897 0.8171

Table A.5 – VAR for eight-month windows

Variables	E_8	D_IPCA_8	Variables	E_8	D_IPCA_8
E_8(-1)	0.7930 (0.0987) [ 8.0398]	0.0016 (0.001) [ 1.6026]	D_IPCA_8(-2)	5.3804 (9.1884) [ 0.5856]	-0.04323 (0.0900) [-0.4790]
E_8(-2)	0.0097 (0.0674) [ 0.1439]	-0.0006 (0.0007) [-0.9426]	C	0.0002 (0.0001) [ 1.8207]	-1.79E-06 (1.1E-06) [-1.63756]
D_IPCA_8(-1)	1.8755 (9.215) [ 0.2035]	0.09867 (0.0903) [ 1.0922]	D2002_M11	0.0015 (0.0005) [ 2.8223]	4.21E-05 (5.2E-06) [ 8.1145]
R-squared	0.721	0.5781	Adj. R-squared	0.6947	0.5383
F-statistic	27.3886	14.5247			

Table A.6 – VAR for twelve-month windows

Variables	E_12	D_IPCA_12	Variables	E_12	D_IPCA_12	Variables	E_12	D_IPCA_12
E_12(-1)	1.1266 (0.1548) [ 7.2795]	0.0066 (0.0017) [ 3.9409]	E_12(-7)	-0.01345 (0.0727) [-0.1849]	0.00166 (0.0008) [ 2.1149]	D_IPCA_12(-6)	6.95244 (8.1141) [ 0.8568]	-0.0856 (0.0874) [-0.9788]
E_12(-2)	-0.0864 (0.2702) [-0.3197]	-0.0041 (0.0029) [-1.394]	D_IPCA_12(-1)	-7.3151 (9.9846) [-0.7326]	0.1543 (0.1076) [ 1.4338]	D_IPCA_12(-7)	-8.1538 (7.6083) [-1.0717]	0.0164 (0.082) [ 0.2005]
E_12(-3)	-0.15121 (0.2749) [-0.5499]	0.0009 (0.003) [ 0.3009]	D_IPCA_12(-2)	5.3827 (9.8458) [ 0.5467]	0.107 (0.1061) [ 1.0081]	C	8.75E-05 (9.6E-05) [ 0.9099]	-1.55E-06 (1.0E-06) [-1.4988]
E_12(-4)	0.1970 (0.2605) [ 0.7565]	-0.0028 (0.0028) [-0.9924]	D_IPCA_12(-3)	-11.8497 (10.5016) [-1.12837]	-0.0342 (0.1132) [-0.3018]	D2002_M11	-0.000391 (0.0003) [-1.1375]	2.64E-05 (3.7E-06) [ 7.1275]
E_12(-5)	-0.1114 (0.2391) [-0.466]	0.0021 (0.0026) [ 0.7939]	D_IPCA_12(-4)	-0.5193 (10.1884) [-0.051]	-0.1149 (0.1098) [-1.0465]	D2003_M10	-0.0018 (0.0004) [-5.0760]	1.46E-05 (3.8E-06) [ 3.8268]
E_12(-6)	0.0218 (0.1654) [ 0.1315]	-0.0040 (0.0018) [-2.2462]	D_IPCA_12(-5)	14.2164 (9.2135) [ 1.543]	0.0848 (0.0993) [ 0.8540]	R-squared Adj. R-squared F-statistic	0.9317 0.8986 28.1265	0.8543 0.7837 12.0931

Table A.7 – ADF Unit Root Test – variances

<i>sample: 2000:03 to 2004:10</i>				
Variable	ADF test statistics	Critical Value at 5%	ADF test statistics – first difference of variables	Critical Value at 5%
p4	-3.2566 <sup>(b)</sup>	-2.9069	-	-
p6	-2.5156 <sup>(b)</sup>	-2.9084	-7.3599	-3.484
p8	-0.8460 <sup>(a)</sup>	-1.9463	-7.3398	-3.4865
p12	-0.4167 <sup>(a)</sup>	-1.9467	-5.9193	-3.4922
e4	-6.5715	-3.4816	-	-
e6	-5.8641 <sup>(b)</sup>	-2.9084	-	-
e8	-5.4361 <sup>(b)</sup>	-2.9100	-	-
e12	-4.5351 <sup>(b)</sup>	-2.9136	-	-

Note: test performed with (a) trend or intercept and (b) without trend

Table A.8 – VAR for four-month windows

Variable	E4	p4	Variables	E4	p4
E4(-1)	0.6525 (0.0605) [ 10.7898]	0.002503 (0.00665) [ 0.37628]	C	0.0088 (0.0032) [ 2.7471]	0.0008 (0.0004) [ 2.1113]
P4(-1)	0.0791 (0.8394) [ 0.0942]	0.700972 (0.09233) [ 7.59224]	R-squared Adj. R-squared F-statistic	0.6643 0.6534 61.3330	0.4998 0.4837 30.976

Note: Std. deviations in parentheses and t-statistics in square brackets.

Table A.9 – VAR for six-month windows

Variable	E6	dp6	Variable	E6	dp6
e6(-1)	0.7630 (0.1127) [ 6.7736]	0.0083 (0.0136) [ 0.6068]	Dp6(-1)	0.7124 (0.8625) [ 0.826]	0.0221 (0.1044) [ 0.2116]
e6(-2)	0.0101 (0.0903) [ 0.1113]	-0.0126 (0.0109) [-1.1549]	Dp6(-2)	0.43334 (0.8515) [ 0.509]	-0.1202 (0.1031) [-1.1664]
C	0.0064 (0.0024) [ 2.6605]	3.82E-05 (0.0003) [ 0.1319]	D2002_M11	0.02998 (0.0077) [ 3.8767]	0.0056 (0.0009) [ 6.0109]
R-squared	0.7255	0.4332	Adj. R-squared	0.7006	0.3817
F-statistic	29.0747	8.4069			

Table A.10 – VAR for eight-month windows

Variable	E8	dp8	Variables	E8	dp8
e8(-1)	0.8994 (0.1177) [ 7.6418]	0.0203 (0.0151) [ 1.3501]	dp8(-1)	0.0669 (1.0564) [ 0.0633]	0.0222 (0.1351) [ 0.1639]
e8(-2)	-0.0595 (0.0988) [-0.6021]	-0.0136 (0.0126) [-1.0740]	dp8(-2)	0.1905 (1.0548) [ 0.1806]	-0.007 (0.1349) [-0.0512]
C	0.0052 (0.0025) [ 2.0663]	-0.0002 (0.0003) [-0.6696]	R-squared	0.7267	0.0338
			Adj. R-squared	0.7064	-0.0378
			F-statistic	35.8896	0.4722

Table A.11 – VAR for twelve-month windows

Variables	E12	dp12	Variables	E12	dp12	Variables	E12	dp12
e12(-1)	0.9752 (0.1086) [ 8.976]	0.0413 (0.0124) [ 3.3225]	dp12(-1)	-0.9046 (1.1596) [-0.7802]	0.1774 (0.1325) [ 1.3391]	C	0.0028 (0.0023) [ 1.2268]	-0.0004 (0.0003) [-1.5782]
e12(-2)	-0.0543 (0.1014) [-0.5357]	-0.0290 (0.0116) [-2.5057]	dp12(-2)	-0.1943 (1.1187) [-0.1736]	0.17707 (0.1278) [ 1.3851]	R-squared	0.8348	0.245
						Adj. R-squared	0.8216	0.1846
						F-statistic	63.1833	4.0552

Table A.12 – Cointegration test between exchange rate and consumer price index

<i>Number of cointegration vectors under Ho</i>	<i>Eigenvalue</i>	<i>Trace statistic</i>	<i>Critical Value ( 5%)</i>	<i>p-value **</i>
<b>Unrestricted Cointegration Rank Test (Trace)</b>				
None	0.1048	8.3109	15.495	0.4328
At most one	0.019	1.2275	3.8412	0.2679
<b>Unrestricted Cointegration Rank Test (Maximum Eigenvalue)</b>				
None	0.1048	7.0834	14.2646	0.4793
At most one	0.019	1.2275	3.8415	0.2679

\*\* MacKinnon-Haug-Michelis (1999) p-values

Table A.13 – Granger Causality Test <sup>22</sup>

Null Hypothesis	Number of Obs.	F-statistic	p-value
E does not Granger-Cause IPCA	66	9.0601	5.0E-05
IPCA does not Granger-Cause E		1.4686	0.2323

Table A.14 – VAR between E and IPCA

Variables	E	IPCA	Variables	E	IPCA
E(-1)	0.6036 (0.1217) [ 4.9597]	0.0356 (0.0111) [ 3.201]	IPCA(-1)	0.9185 (1.2735) [ 0.7213]	0.6556 (0.1163) [ 5.6392]
E(-2)	-0.1168 (0.1501) [-0.7780]	-0.0037 (0.0137) [-0.2669]	IPCA(-2)	-2.704 (1.5498) [-1.7447]	-0.2059 (0.1415) [-1.4555]
E(-3)	0.1183 (0.1239) [ 0.9547]	0.0220 (0.0113) [ 1.9463]	IPCA(-3)	2.4593 (1.5498) [ 1.5868]	0.1452 (0.1415) [ 1.0260]
E(-4)	0.0827 (0.1033) [ 0.8007]	-0.0051 (0.0094) [-0.5394]	IPCA(-4)	-2.5399 (1.1504) [-2.2079]	0.06289 (0.1050) [ 0.5988]
C	0.01652 (0.0084) [ 1.9756]	0.0018 (0.0008) [ 2.3730]	D2002_M11	-0.135 (0.0344) [-3.9256]	0.0143 (0.0031) [ 4.5682]
R-squared	0.4582	0.7168	Adj. R-squared	0.3696	0.6704
F-statistic	5.1688	15.4665			

Note: Std. deviations in parenthesis and t-statistics in square brackets.

Table A.15 – Variance Decomposition (Cholesky ordering: E IPCA)

Variance decomposition of E:				Variance decomposition of IPCA:			
Period	Std. Error	E	IPCA	Period	Std. Error	E	IPCA
1	0.0306	100.000	0.0000	1	0.0028	3.0385	96.9616
2	0.0356	99.4964	0.5036	2	0.0034	7.1131	92.8869
3	0.0370	98.2151	1.7849	3	0.0037	15.7357	84.2643
4	0.0374	98.2384	1.7616	4	0.004	27.0031	72.997
5	0.0383	97.469	2.5310	5	0.0042	32.3807	67.6193
6	0.0391	95.4898	4.5102	6	0.0043	36.3763	63.6237
7	0.0395	93.5715	6.4285	7	0.0044	39.2664	60.7336
8	0.0397	92.8832	7.1168	8	0.0045	41.3734	58.6266
9	0.0398	92.2703	7.7298	9	0.0046	42.3243	57.6758
10	0.0400	91.7409	8.2591	10	0.0046	42.5519	57.4481
11	0.0402	91.4451	8.5549	11	0.0046	42.4477	57.5523
12	0.0403	91.3992	8.6008	12	0.0046	42.2399	57.7601

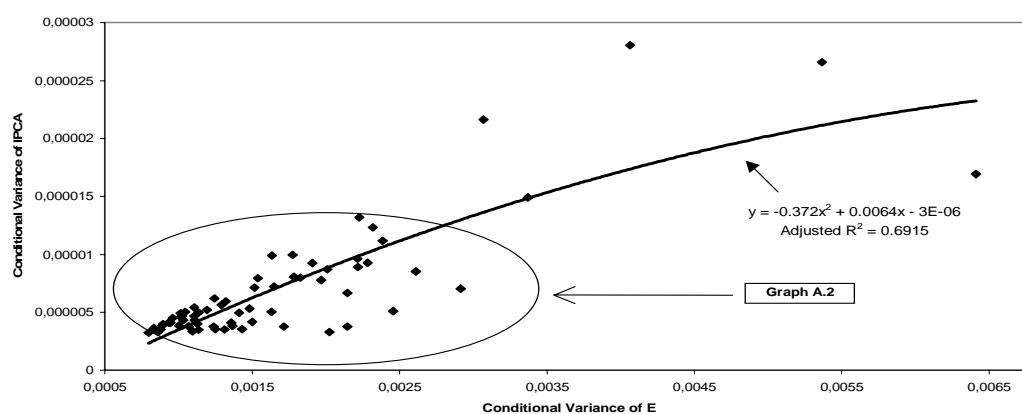
<sup>22</sup> It is important to include as many lags as possible in variable  $x$  that may be significant over variable  $y$ . We tested an equation with 13 lags in both variables and the highest significant lag of  $x$  over  $y$  was the third lag of E over IPCA. In the Granger Causality test the null hypothesis that IPCA Granger-Causes E is rejected both with 3 and with 13 lags.

Table A.16 - OLS Equation for E

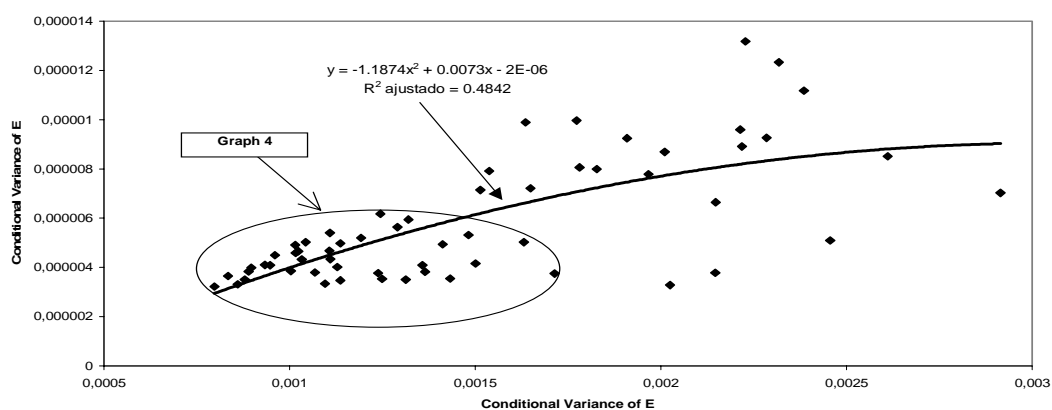
Variable	Coefficient	Standard Error	t-statistic	p-value
C	0.0059	0.0092	0.6378	0.5258
AR(1)	0.4341	0.0964	4.5041	0.0000
R <sup>2</sup>	0.2351	LM Test (1 lag) <sup>(a)</sup>		0.8708
Adjusted R <sup>2</sup>	0.2235	ARCH-LM Test (1 lag)		28.6673 <sup>(b)</sup>

Note: (a) null hypothesis of absence of autocorrelation accepted also for higher number of lags; (b) null hypothesis of absence of ARCH residuals rejected at 1%.

Graph A.1 — Exchange rate and inflation volatilities (reduced sample)

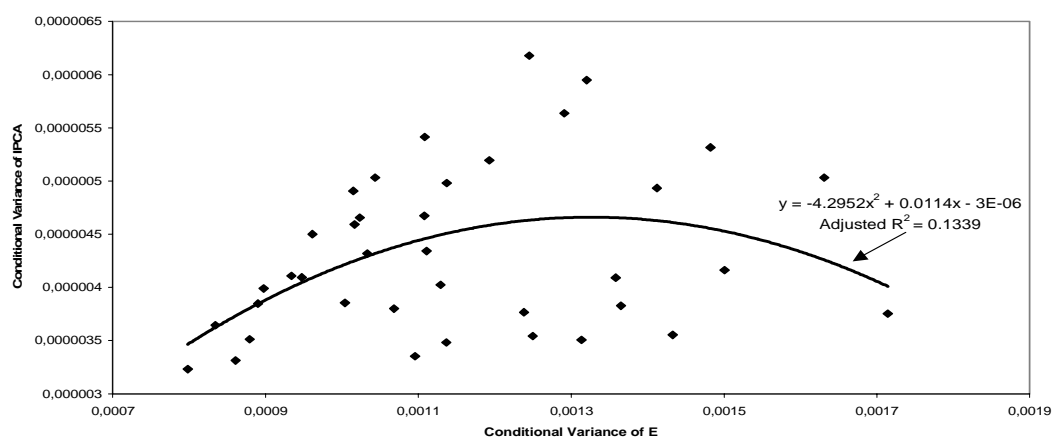


Graph A.2 — Exchange rate and inflation volatilities (reduced sample)





Graph A.3 — Exchange rate and inflation volatilities (reduced sample)



## Appendix II – Diagnostic Tests for the Bi-Garch Model

This appendix brings a brief explanation about the test of covariance stationarity in the multivariate Garch model under the BEKK restriction. For details, see ENGLE and KRONER (1993).

In a bivariate GARCH (1,1), the conditional variance has the form:

$$\begin{bmatrix} u_{1t}^2 \\ u_{2t}^2 \\ u_{2t}^2 \end{bmatrix} = \begin{bmatrix} c_{11} \\ c_{12} \\ c_{22} \end{bmatrix} + \begin{bmatrix} B_{11} & B_{12} & B_{13} \\ B_{21} & B_{22} & B_{23} \\ B_{31} & B_{32} & B_{33} \end{bmatrix} \begin{bmatrix} \sigma_{11}^2(t-1) \\ \sigma_{12}^2(t-1) \\ \sigma_{22}^2(t-1) \end{bmatrix} + \begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix} \begin{bmatrix} u_{1(t-1)}^2 \\ u_{2(t-1)}^2 \\ u_{2(t-1)}^2 \end{bmatrix}$$

Without exogenous variables, the BEKK restriction has the form:

$$U_t = C_1^* C_1^* + \begin{bmatrix} B_{11}^* & B_{12}^* \\ B_{21}^* & B_{22}^* \end{bmatrix} \begin{bmatrix} \sigma_{1,t-1}^2 & \sigma_{1,t-1} \sigma_{2,t-1} \\ \sigma_{2,t-1} \sigma_{1,t-1} & \sigma_{2,t-1}^2 \end{bmatrix} \begin{bmatrix} B_{11}^* & B_{12}^* \\ B_{21}^* & B_{22}^* \end{bmatrix} + \begin{bmatrix} A_{11}^* & A_{12}^* \\ A_{21}^* & A_{22}^* \end{bmatrix} [U_{t-1}] \begin{bmatrix} A_{11}^* & A_{12}^* \\ A_{21}^* & A_{22}^* \end{bmatrix}$$

To assure the process is covariance stationary, the *eigenvalues* of  $\sum_{i=1}^q \sum_{k=1}^K (B_{ik}^* \otimes B_{ik}^*) + \sum_{i=1}^p \sum_{k=1}^K (A_{ik} \otimes A_{ik})$  must be minor than the unity, in absolute values. In other words,

we have to calculate the eigenvalue of matrix X below:

$$X = \begin{bmatrix} (a_{11} * a_{11}) + (g_{11} * g_{11}) & (a_{11} * a_{12}) + (g_{11} * g_{12}) & (a_{12} * a_{11}) + (g_{12} * g_{11}) & (a_{12} * a_{12}) + (g_{12} * g_{12}) \\ (a_{21} * a_{11}) + (g_{21} * g_{11}) & (a_{11} * a_{22}) + (g_{11} * g_{12}) & (a_{12} * a_{21}) + (g_{12} * g_{21}) & (g_{12} * g_{22}) + (g_{12} * g_{21}) \\ (a_{21} * a_{11}) + (g_{21} * g_{11}) & (a_{21} * a_{12}) + (g_{21} * g_{12}) & (a_{22} * a_{11}) + (g_{22} * g_{11}) & (a_{22} * a_{12}) + (g_{22} * g_{12}) \\ (a_{21} * a_{21}) + (g_{21} * g_{21}) & (a_{21} * a_{22}) + (g_{21} * g_{22}) & (a_{21} * a_{22}) + (g_{21} * g_{22}) & (a_{22} * a_{22}) + (g_{22} * g_{22}) \end{bmatrix}$$

Calculating the eigenvalues of X using the coefficients for case 2 presented in table 3 along the text, we find the vector y of eigenvalues presented in table 8, where all absolute values are minor than one. Hence, the case chosen respect the condition of covariance stationarity.

# Banco Central do Brasil

## Trabalhos para Discussão

*Os Trabalhos para Discussão podem ser acessados na internet, no formato PDF, no endereço: <http://www.bc.gov.br>*

## Working Paper Series

*Working Papers in PDF format can be downloaded from: <http://www.bc.gov.br>*

- |           |   |          |
|-----------|---|----------|
| <b>1</b>  | <b>Implementing Inflation Targeting in Brazil</b><br><i>Joel Bogdanski, Alexandre Antonio Tombini and Sérgio Ribeiro da Costa Werlang</i>   | Jul/2000 |
| <b>2</b>  | <b>Política Monetária e Supervisão do Sistema Financeiro Nacional no Banco Central do Brasil</b><br><i>Eduardo Lundberg</i>   | Jul/2000 |
|           | <b>Monetary Policy and Banking Supervision Functions on the Central Bank</b><br><i>Eduardo Lundberg</i>   | Jul/2000 |
| <b>3</b>  | <b>Private Sector Participation: a Theoretical Justification of the Brazilian Position</b><br><i>Sérgio Ribeiro da Costa Werlang</i>  | Jul/2000 |
| <b>4</b>  | <b>An Information Theory Approach to the Aggregation of Log-Linear Models</b><br><i>Pedro H. Albuquerque</i>  | Jul/2000 |
| <b>5</b>  | <b>The Pass-Through from Depreciation to Inflation: a Panel Study</b><br><i>Ilan Goldfajn and Sérgio Ribeiro da Costa Werlang</i>   | Jul/2000 |
| <b>6</b>  | <b>Optimal Interest Rate Rules in Inflation Targeting Frameworks</b><br><i>José Alvaro Rodrigues Neto, Fabio Araújo and Marta Baltar J. Moreira</i>   | Jul/2000 |
| <b>7</b>  | <b>Leading Indicators of Inflation for Brazil</b><br><i>Marcelle Chauvet</i>  | Sep/2000 |
| <b>8</b>  | <b>The Correlation Matrix of the Brazilian Central Bank's Standard Model for Interest Rate Market Risk</b><br><i>José Alvaro Rodrigues Neto</i>   | Sep/2000 |
| <b>9</b>  | <b>Estimating Exchange Market Pressure and Intervention Activity</b><br><i>Emanuel-Werner Kohlscheen</i>  | Nov/2000 |
| <b>10</b> | <b>Análise do Financiamento Externo a uma Pequena Economia<br/>Aplicação da Teoria do Prêmio Monetário ao Caso Brasileiro: 1991–1998</b><br><i>Carlos Hamilton Vasconcelos Araújo e Renato Galvão Flôres Júnior</i> | Mar/2001 |
| <b>11</b> | <b>A Note on the Efficient Estimation of Inflation in Brazil</b><br><i>Michael F. Bryan and Stephen G. Cecchetti</i>  | Mar/2001 |
| <b>12</b> | <b>A Test of Competition in Brazilian Banking</b><br><i>Márcio I. Nakane</i>  | Mar/2001 |

13	<b>Modelos de Previsão de Insolvência Bancária no Brasil</b> <i>Marcio Magalhães Janot</i>	Mar/2001
14	<b>Evaluating Core Inflation Measures for Brazil</b> <i>Francisco Marcos Rodrigues Figueiredo</i>	Mar/2001
15	<b>Is It Worth Tracking Dollar/Real Implied Volatility?</b> <i>Sandro Canesso de Andrade and Benjamin Miranda Tabak</i>	Mar/2001
16	<b>Avaliação das Projeções do Modelo Estrutural do Banco Central do Brasil para a Taxa de Variação do IPCA</b> <i>Sergio Afonso Lago Alves</i>	Mar/2001
	<b>Evaluation of the Central Bank of Brazil Structural Model's Inflation Forecasts in an Inflation Targeting Framework</b> <i>Sergio Afonso Lago Alves</i>	Jul/2001
17	<b>Estimando o Produto Potencial Brasileiro: uma Abordagem de Função de Produção</b> <i>Tito Nícias Teixeira da Silva Filho</i>	Abr/2001
	<b>Estimating Brazilian Potential Output: a Production Function Approach</b> <i>Tito Nícias Teixeira da Silva Filho</i>	Aug/2002
18	<b>A Simple Model for Inflation Targeting in Brazil</b> <i>Paulo Springer de Freitas and Marcelo Kfoury Muinhos</i>	Apr/2001
19	<b>Uncovered Interest Parity with Fundamentals: a Brazilian Exchange Rate Forecast Model</b> <i>Marcelo Kfoury Muinhos, Paulo Springer de Freitas and Fabio Araújo</i>	May/2001
20	<b>Credit Channel without the LM Curve</b> <i>Victorio Y. T. Chu and Márcio I. Nakane</i>	May/2001
21	<b>Os Impactos Econômicos da CPMF: Teoria e Evidência</b> <i>Pedro H. Albuquerque</i>	Jun/2001
22	<b>Decentralized Portfolio Management</b> <i>Paulo Coutinho and Benjamin Miranda Tabak</i>	Jun/2001
23	<b>Os Efeitos da CPMF sobre a Intermediação Financeira</b> <i>Sérgio Mikio Koyama e Márcio I. Nakane</i>	Jul/2001
24	<b>Inflation Targeting in Brazil: Shocks, Backward-Looking Prices, and IMF Conditionality</b> <i>Joel Bogdanski, Paulo Springer de Freitas, Ilan Goldfajn and Alexandre Antonio Tombini</i>	Aug/2001
25	<b>Inflation Targeting in Brazil: Reviewing Two Years of Monetary Policy 1999/00</b> <i>Pedro Fachada</i>	Aug/2001
26	<b>Inflation Targeting in an Open Financially Integrated Emerging Economy: the Case of Brazil</b> <i>Marcelo Kfoury Muinhos</i>	Aug/2001
27	<b>Complementaridade e Fungibilidade dos Fluxos de Capitais Internacionais</b> <i>Carlos Hamilton Vasconcelos Araújo e Renato Galvão Flôres Júnior</i>	Set/2001

28	<b>Regras Monetárias e Dinâmica Macroeconômica no Brasil: uma Abordagem de Expectativas Racionais</b> <i>Marco Antonio Bonomo e Ricardo D. Brito</i>	Nov/2001
29	<b>Using a Money Demand Model to Evaluate Monetary Policies in Brazil</b> <i>Pedro H. Albuquerque and Solange Gouvêa</i>	Nov/2001
30	<b>Testing the Expectations Hypothesis in the Brazilian Term Structure of Interest Rates</b> <i>Benjamin Miranda Tabak and Sandro Canesso de Andrade</i>	Nov/2001
31	<b>Algumas Considerações sobre a Sazonalidade no IPCA</b> <i>Francisco Marcos R. Figueiredo e Roberta Blass Staub</i>	Nov/2001
32	<b>Crises Cambiais e Ataques Especulativos no Brasil</b> <i>Mauro Costa Miranda</i>	Nov/2001
33	<b>Monetary Policy and Inflation in Brazil (1975-2000): a VAR Estimation</b> <i>André Minella</i>	Nov/2001
34	<b>Constrained Discretion and Collective Action Problems: Reflections on the Resolution of International Financial Crises</b> <i>Arminio Fraga and Daniel Luiz Gleizer</i>	Nov/2001
35	<b>Uma Definição Operacional de Estabilidade de Preços</b> <i>Tito Nícias Teixeira da Silva Filho</i>	Dez/2001
36	<b>Can Emerging Markets Float? Should They Inflation Target?</b> <i>Barry Eichengreen</i>	Feb/2002
37	<b>Monetary Policy in Brazil: Remarks on the Inflation Targeting Regime, Public Debt Management and Open Market Operations</b> <i>Luiz Fernando Figueiredo, Pedro Fachada and Sérgio Goldenstein</i>	Mar/2002
38	<b>Volatilidade Implícita e Antecipação de Eventos de Stress: um Teste para o Mercado Brasileiro</b> <i>Frederico Pechir Gomes</i>	Mar/2002
39	<b>Opções sobre Dólar Comercial e Expectativas a Respeito do Comportamento da Taxa de Câmbio</b> <i>Paulo Castor de Castro</i>	Mar/2002
40	<b>Speculative Attacks on Debts, Dollarization and Optimum Currency Areas</b> <i>Aloisio Araujo and Márcia Leon</i>	Apr/2002
41	<b>Mudanças de Regime no Câmbio Brasileiro</b> <i>Carlos Hamilton V. Araújo e Getúlio B. da Silveira Filho</i>	Jun/2002
42	<b>Modelo Estrutural com Setor Externo: Endogenização do Prêmio de Risco e do Câmbio</b> <i>Marcelo Kfoury Muinhos, Sérgio Afonso Lago Alves e Gil Riella</i>	Jun/2002
43	<b>The Effects of the Brazilian ADRs Program on Domestic Market Efficiency</b> <i>Benjamin Miranda Tabak and Eduardo José Araújo Lima</i>	Jun/2002

<b>44</b>	<b>Estrutura Competitiva, Produtividade Industrial e Liberação Comercial no Brasil</b> <i>Pedro Cavalcanti Ferreira e Osmani Teixeira de Carvalho Guillén</i>	Jun/2002
<b>45</b>	<b>Optimal Monetary Policy, Gains from Commitment, and Inflation Persistence</b> <i>André Minella</i>	Aug/2002
<b>46</b>	<b>The Determinants of Bank Interest Spread in Brazil</b> <i>Tarsila Segalla Afanasieff, Priscilla Maria Villa Lhacer and Márcio I. Nakane</i>	Aug/2002
<b>47</b>	<b>Indicadores Derivados de Agregados Monetários</b> <i>Fernando de Aquino Fonseca Neto e José Albuquerque Júnior</i>	Set/2002
<b>48</b>	<b>Should Government Smooth Exchange Rate Risk?</b> <i>Ilan Goldfajn and Marcos Antonio Silveira</i>	Sep/2002
<b>49</b>	<b>Desenvolvimento do Sistema Financeiro e Crescimento Econômico no Brasil: Evidências de Causalidade</b> <i>Orlando Carneiro de Matos</i>	Set/2002
<b>50</b>	<b>Macroeconomic Coordination and Inflation Targeting in a Two-Country Model</b> <i>Eui Jung Chang, Marcelo Kfoury Muinhos and Joanílio Rodolpho Teixeira</i>	Sep/2002
<b>51</b>	<b>Credit Channel with Sovereign Credit Risk: an Empirical Test</b> <i>Victorio Yi Tson Chu</i>	Sep/2002
<b>52</b>	<b>Generalized Hyperbolic Distributions and Brazilian Data</b> <i>José Fajardo and Aquiles Farias</i>	Sep/2002
<b>53</b>	<b>Inflation Targeting in Brazil: Lessons and Challenges</b> <i>André Minella, Paulo Springer de Freitas, Ilan Goldfajn and Marcelo Kfoury Muinhos</i>	Nov/2002
<b>54</b>	<b>Stock Returns and Volatility</b> <i>Benjamin Miranda Tabak and Solange Maria Guerra</i>	Nov/2002
<b>55</b>	<b>Componentes de Curto e Longo Prazo das Taxas de Juros no Brasil</b> <i>Carlos Hamilton Vasconcelos Araújo e Osmani Teixeira de Carvalho de Guillén</i>	Nov/2002
<b>56</b>	<b>Causality and Cointegration in Stock Markets: the Case of Latin America</b> <i>Benjamin Miranda Tabak and Eduardo José Araújo Lima</i>	Dec/2002
<b>57</b>	<b>As Leis de Falência: uma Abordagem Econômica</b> <i>Aloisio Araujo</i>	Dez/2002
<b>58</b>	<b>The Random Walk Hypothesis and the Behavior of Foreign Capital Portfolio Flows: the Brazilian Stock Market Case</b> <i>Benjamin Miranda Tabak</i>	Dec/2002
<b>59</b>	<b>Os Preços Administrados e a Inflação no Brasil</b> <i>Francisco Marcos R. Figueiredo e Thaís Porto Ferreira</i>	Dez/2002
<b>60</b>	<b>Delegated Portfolio Management</b> <i>Paulo Coutinho and Benjamin Miranda Tabak</i>	Dec/2002

61	<b>O Uso de Dados de Alta Frequência na Estimação da Volatilidade e do Valor em Risco para o Ibovespa</b> <i>João Maurício de Souza Moreira e Eduardo Facó Lemgruber</i>	Dez/2002
62	<b>Taxa de Juros e Concentração Bancária no Brasil</b> <i>Eduardo Kiyoshi Tonooka e Sérgio Mikio Koyama</i>	Fev/2003
63	<b>Optimal Monetary Rules: the Case of Brazil</b> <i>Charles Lima de Almeida, Marco Aurélio Peres, Geraldo da Silva e Souza and Benjamin Miranda Tabak</i>	Fev/2003
64	<b>Medium-Size Macroeconomic Model for the Brazilian Economy</b> <i>Marcelo Kfoury Muinhos and Sergio Afonso Lago Alves</i>	Fev/2003
65	<b>On the Information Content of Oil Future Prices</b> <i>Benjamin Miranda Tabak</i>	Fev/2003
66	<b>A Taxa de Juros de Equilíbrio: uma Abordagem Múltipla</b> <i>Pedro Calhman de Miranda e Marcelo Kfoury Muinhos</i>	Fev/2003
67	<b>Avaliação de Métodos de Cálculo de Exigência de Capital para Risco de Mercado de Carteiras de Ações no Brasil</b> <i>Gustavo S. Araújo, João Maurício S. Moreira e Ricardo S. Maia Clemente</i>	Fev/2003
68	<b>Real Balances in the Utility Function: Evidence for Brazil</b> <i>Leonardo Soriano de Alencar and Márcio I. Nakane</i>	Fev/2003
69	<b>r-filters: a Hodrick-Prescott Filter Generalization</b> <i>Fabio Araújo, Marta Baltar Moreira Areosa and José Alvaro Rodrigues Neto</i>	Fev/2003
70	<b>Monetary Policy Surprises and the Brazilian Term Structure of Interest Rates</b> <i>Benjamin Miranda Tabak</i>	Fev/2003
71	<b>On Shadow-Prices of Banks in Real-Time Gross Settlement Systems</b> <i>Rodrigo Penaloza</i>	Apr/2003
72	<b>O Prêmio pela Maturidade na Estrutura a Termo das Taxas de Juros Brasileiras</b> <i>Ricardo Dias de Oliveira Brito, Angelo J. Mont'Alverne Duarte e Osmani Teixeira de C. Guillen</i>	Maio/2003
73	<b>Análise de Componentes Principais de Dados Funcionais – Uma Aplicação às Estruturas a Termo de Taxas de Juros</b> <i>Getúlio Borges da Silveira e Octavio Bessada</i>	Maio/2003
74	<b>Aplicação do Modelo de Black, Derman &amp; Toy à Precificação de Opções Sobre Títulos de Renda Fixa</b> <i>Octavio Manuel Bessada Lion, Carlos Alberto Nunes Cosenza e César das Neves</i>	Maio/2003
75	<b>Brazil's Financial System: Resilience to Shocks, no Currency Substitution, but Struggling to Promote Growth</b> <i>Ilan Goldfajn, Katherine Hennings and Helio Mori</i>	Jun/2003

<b>76</b>	<b>Inflation Targeting in Emerging Market Economies</b> <i>Arminio Fraga, Ilan Goldfajn and André Minella</i>	Jun/2003
<b>77</b>	<b>Inflation Targeting in Brazil: Constructing Credibility under Exchange Rate Volatility</b> <i>André Minella, Paulo Springer de Freitas, Ilan Goldfajn and Marcelo Kfoury Muinhos</i>	Jul/2003
<b>78</b>	<b>Contornando os Pressupostos de Black &amp; Scholes: Aplicação do Modelo de Precificação de Opções de Duan no Mercado Brasileiro</b> <i>Gustavo Silva Araújo, Claudio Henrique da Silveira Barbedo, Antonio Carlos Figueiredo, Eduardo Facó Lemgruber</i>	Out/2003
<b>79</b>	<b>Inclusão do Decaimento Temporal na Metodologia Delta-Gama para o Cálculo do VaR de Carteiras Compradas em Opções no Brasil</b> <i>Claudio Henrique da Silveira Barbedo, Gustavo Silva Araújo, Eduardo Facó Lemgruber</i>	Out/2003
<b>80</b>	<b>Diferenças e Semelhanças entre Países da América Latina: uma Análise de <i>Markov Switching</i> para os Ciclos Econômicos de Brasil e Argentina</b> <i>Arnildo da Silva Correa</i>	Out/2003
<b>81</b>	<b>Bank Competition, Agency Costs and the Performance of the Monetary Policy</b> <i>Leonardo Soriano de Alencar and Márcio I. Nakane</i>	Jan/2004
<b>82</b>	<b>Carteiras de Opções: Avaliação de Metodologias de Exigência de Capital no Mercado Brasileiro</b> <i>Cláudio Henrique da Silveira Barbedo e Gustavo Silva Araújo</i>	Mar/2004
<b>83</b>	<b>Does Inflation Targeting Reduce Inflation? An Analysis for the OECD Industrial Countries</b> <i>Thomas Y. Wu</i>	May/2004
<b>84</b>	<b>Speculative Attacks on Debts and Optimum Currency Area: A Welfare Analysis</b> <i>Aloisio Araujo and Marcia Leon</i>	May/2004
<b>85</b>	<b>Risk Premia for Emerging Markets Bonds: Evidence from Brazilian Government Debt, 1996-2002</b> <i>André Soares Loureiro and Fernando de Holanda Barbosa</i>	May/2004
<b>86</b>	<b>Identificação do Fator Estocástico de Descontos e Algumas Implicações sobre Testes de Modelos de Consumo</b> <i>Fabio Araujo e João Victor Issler</i>	Mai/2004
<b>87</b>	<b>Mercado de Crédito: uma Análise Econométrica dos Volumes de Crédito Total e Habitacional no Brasil</b> <i>Ana Carla Abrão Costa</i>	Dez/2004
<b>88</b>	<b>Ciclos Internacionais de Negócios: uma Análise de Mudança de Regime Markoviano para Brasil, Argentina e Estados Unidos</b> <i>Arnildo da Silva Correa e Ronald Otto Hillbrecht</i>	Dez/2004
<b>89</b>	<b>O Mercado de <i>Hedge</i> Cambial no Brasil: Reação das Instituições Financeiras a Intervenções do Banco Central</b> <i>Fernando N. de Oliveira</i>	Dez/2004



<b>90</b>	<b>Bank Privatization and Productivity: Evidence for Brazil</b> <i>Márcio I. Nakane and Daniela B. Weintraub</i>	Dec/2004
<b>91</b>	<b>Credit Risk Measurement and the Regulation of Bank Capital and Provision Requirements in Brazil – A Corporate Analysis</b> <i>Ricardo Schechtman, Valéria Salomão Garcia, Sergio Mikio Koyama and Guilherme Cronemberger Parente</i>	Dec/2004
<b>92</b>	<b>Steady-State Analysis of an Open Economy General Equilibrium Model for Brazil</b> <i>Mirta Noemi Sataka Bugarin, Roberto de Goes Ellery Jr., Victor Gomes Silva, Marcelo Kfoury Muinhos</i>	Apr/2005
<b>93</b>	<b>Avaliação de Modelos de Cálculo de Exigência de Capital para Risco Cambial</b> <i>Claudio H. da S. Barbedo, Gustavo S. Araújo, João Maurício S. Moreira e Ricardo S. Maia Clemente</i>	Abr/2005
<b>94</b>	<b>Simulação Histórica Filtrada: Incorporação da Volatilidade ao Modelo Histórico de Cálculo de Risco para Ativos Não-Lineares</b> <i>Claudio Henrique da Silveira Barbedo, Gustavo Silva Araújo e Eduardo Facó Lemgruber</i>	Abr/2005
<b>95</b>	<b>Comment on Market Discipline and Monetary Policy by Carl Walsh</b> <i>Maurício S. Bugarin and Fábila A. de Carvalho</i>	Apr/2005
<b>96</b>	<b>O que É Estratégia: uma Abordagem Multiparadigmática para a Disciplina</b> <i>Anthero de Moraes Meirelles</i>	Ago/2005
<b>97</b>	<b>Finance and the Business Cycle: a Kalman Filter Approach with Markov Switching</b> <i>Ryan A. Compton and Jose Ricardo da Costa e Silva</i>	Aug/2005
<b>98</b>	<b>Capital Flows Cycle: Stylized Facts and Empirical Evidences for Emerging Market Economies</b> <i>Helio Mori e Marcelo Kfoury Muinhos</i>	Aug/2005
<b>99</b>	<b>Adequação das Medidas de Valor em Risco na Formulação da Exigência de Capital para Estratégias de Opções no Mercado Brasileiro</b> <i>Gustavo Silva Araújo, Claudio Henrique da Silveira Barbedo, e Eduardo Facó Lemgruber</i>	Set/2005
<b>100</b>	<b>Targets and Inflation Dynamics</b> <i>Sergio A. L. Alves and Waldyr D. Areosa</i>	Oct/2005
<b>101</b>	<b>Comparing Equilibrium Real Interest Rates: Different Approaches to Measure Brazilian Rates</b> <i>Marcelo Kfoury Muinhos and Márcio I. Nakane</i>	Mar/2006

- |            |  |          |
|------------|--|----------|
| <b>102</b> | <b>Judicial Risk and Credit Market Performance: Micro Evidence from Brazilian Payroll Loans</b><br><i>Ana Carla A. Costa and João M. P. de Mello</i>                             | Apr/2006 |
| <b>103</b> | <b>The Effect of Adverse Supply Shocks on Monetary Policy and Output</b><br><i>Maria da Glória D. S. Araújo, Mirta Bugarin, Marcelo Kfoury Muinhos and Jose Ricardo C. Silva</i> | Apr/2006 |
| <b>104</b> | <b>Extração de Informação de Opções Cambiais no Brasil</b><br><i>Eui Jung Chang e Benjamin Miranda Tabak</i>   | Apr/2006 |
| <b>105</b> | <b>Representing Roommate's Preferences with Symmetric Utilities</b><br><i>José Alvaro Rodrigues-Neto</i>   | Apr/2006 |